

# Computational Methods for Kinetic Processes in Plasma Physics



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June 2, 2015

# *Context*

- History of Tristan code
- Major differences with other PIC codes
- Applications of Tristan code
- Structure of Tristan code

Subroutines

- Initial settings

Jet simulations

Reconnections

## ***History of Tristan code***

- 1989: working on the old code written by the assembler language for Cray 1 by Oscar Buneman (failed)
- 1990: Tri-dimensional Stanford (Tristan) code is developed for solar wind-magnetosphere interaction
- 1993: Oscar Buneman passed away on January 24 and ***Computer Space Plasma Physics: Simulation Techniques and Software*** was published April
- 1993 – 2001: Global solar wind-magnetosphere interaction was investigated with interstellar magnetic fields (IMFs)
- 1995: thin jet simulations have been performed
- 2002 – present: Weibel (filamentation) instability has been investigated
- 2006 – present: reconnection simulations have been performed
- 2008: The TristanMPI has been developed by Jacek Niemiec when he was at Iowa State University first used for the investigation of Cosmic ray acceleration
- 2008 – present: Synthetic radiation has been investigated

## ***Major differences with other PIC codes***

UPIC: spectral method  
in general good for avoiding numerical Cherenkov radiation

Tristan: conserving current deposit  
good for MPI and non-periodic boundary conditions

## ***Applications of Tristan code***

Global solar wind-magnetosphere interaction

Relativistic jets

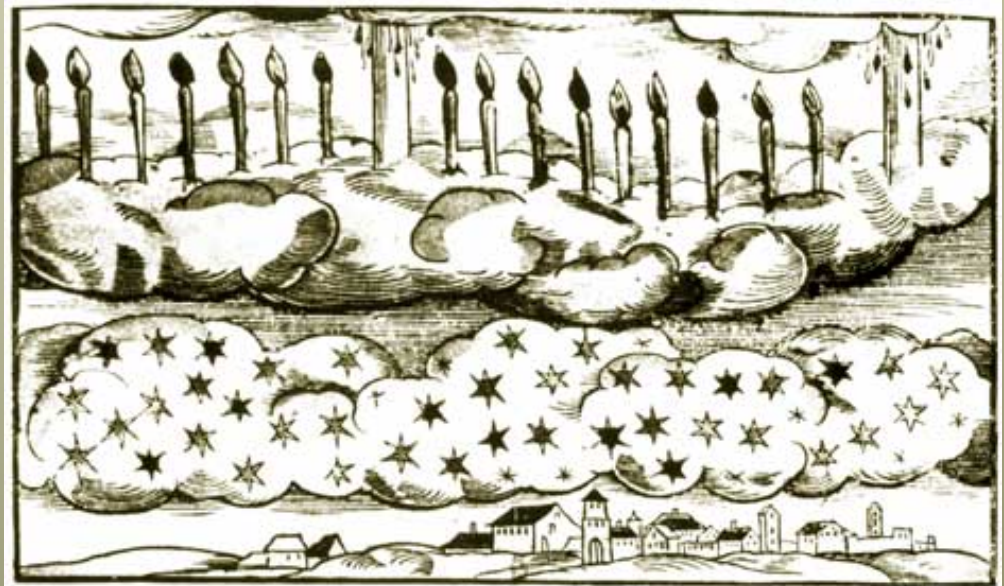
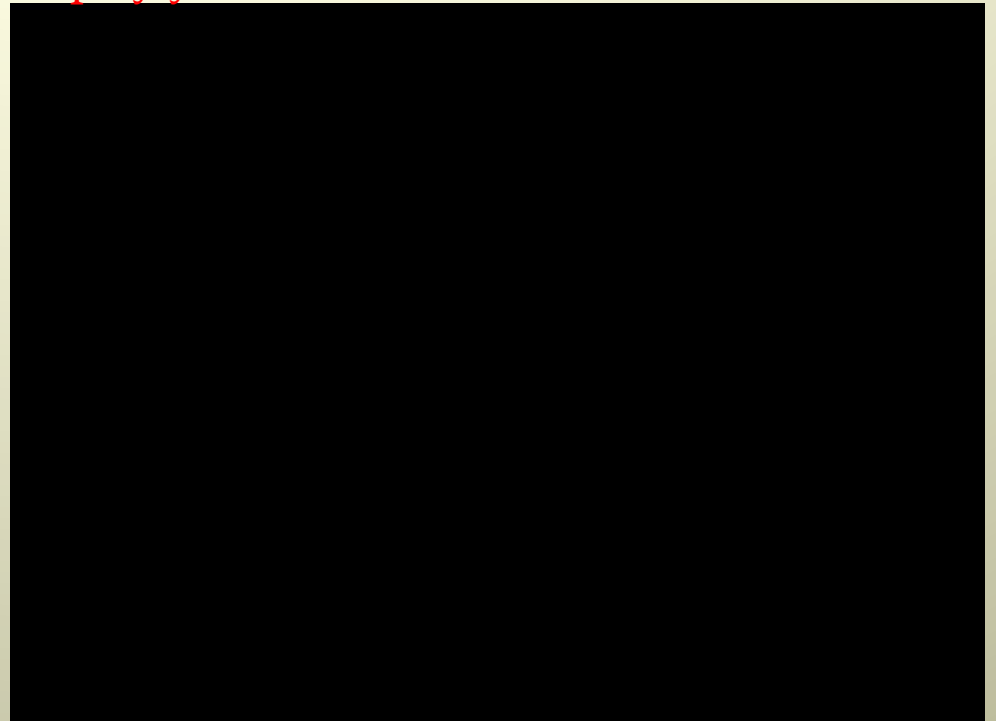
Kinetic Kelvin-Helmholtz instability (kKHI)

# Outline of talk

- ⦿ Space Weather research
  - ⦿ Reconnection in magnetosphere with IMF
    - \* southward IMF
    - \* duskward IMF
  - ⦿ Reconnection in astrophysics
    - \* Mini-jets in Relativistic jets
    - \* Pulsar Nebula
  - ⦿ New aspects of reconnection in astrophysical jets
    - \* additional acceleration mechanism
    - \* radiation mechanism for gamma-ray burst?
  - ⦿ Summary
- (Courtesy of J. Raeder for some slides)

# Aurora

- Hard to sell space physics: there is not much to see, unlike astronomy!
- Only at high latitudes: aurora: the TV screen of the magnetosphere.
- Rarely at low latitudes: geomagnetic storms (1989, 2003). Quite frightening for people in ancient times.
- Even many scientists who study space physics have not seen aurorae! Thankfully, we have conferences:
- 1994: ICS2, Fairbanks, AK: very active.
- 2007: ESA/CLUSTER workshop, Saariselka, Lapland: solar minimum, dooh!
- 2011: Chapman conference, Fairbanks, AK: better now!
- Always: cold (-30C) because you can't see them in daylight.

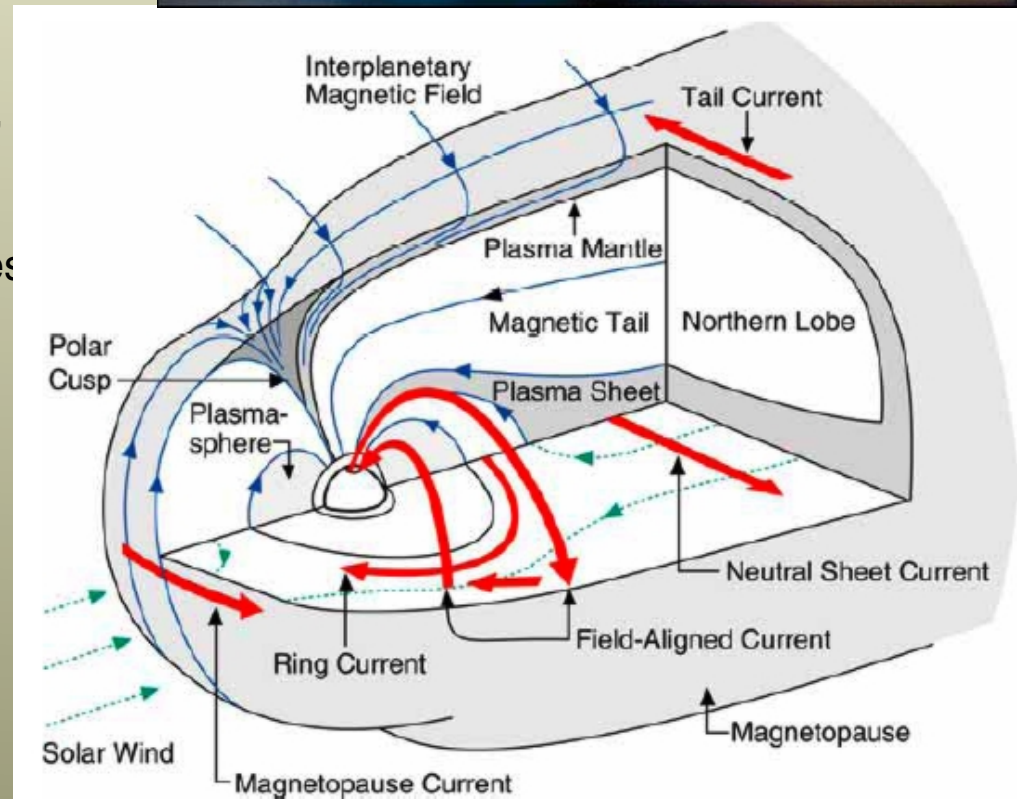
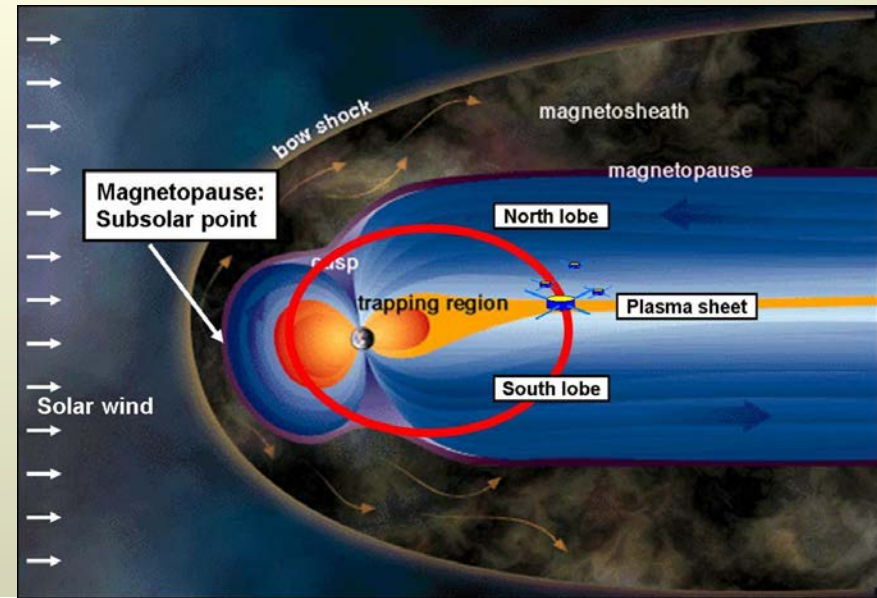


# Geospace

After 50+ years of space research and ~100 satellite missions we can draw some pictures and name features and processes:

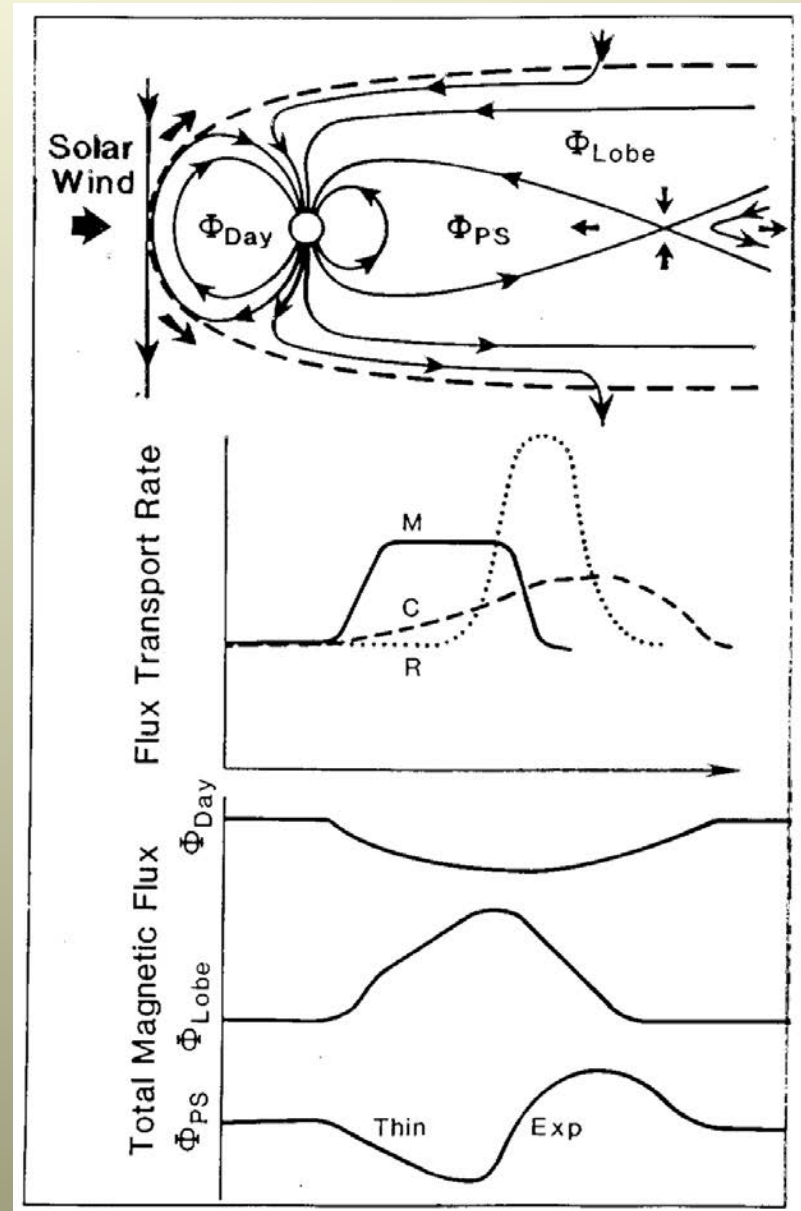
Solar Wind / IMF, bow shock, magnetosheath, magnetopause, reconnection, cusps, boundary layers, tail lobes, plasma sheet, neutral sheet, ring current, radiation belts, field aligned currents, auroral particle precipitation, ionosphere convection, ionosphere layers, TEC, ionosphere currents, ion outflow, thermosphere/density, thermosphere composition, thermosphere winds and tides .....

Lots of features and processes. Our understanding of how everything works together is still mostly at the cartoon level. We can not claim understanding until we have predictive models.



# So, why does the aurora light up: Substorms

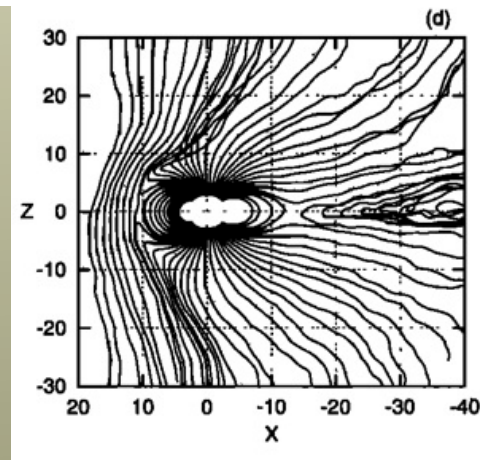
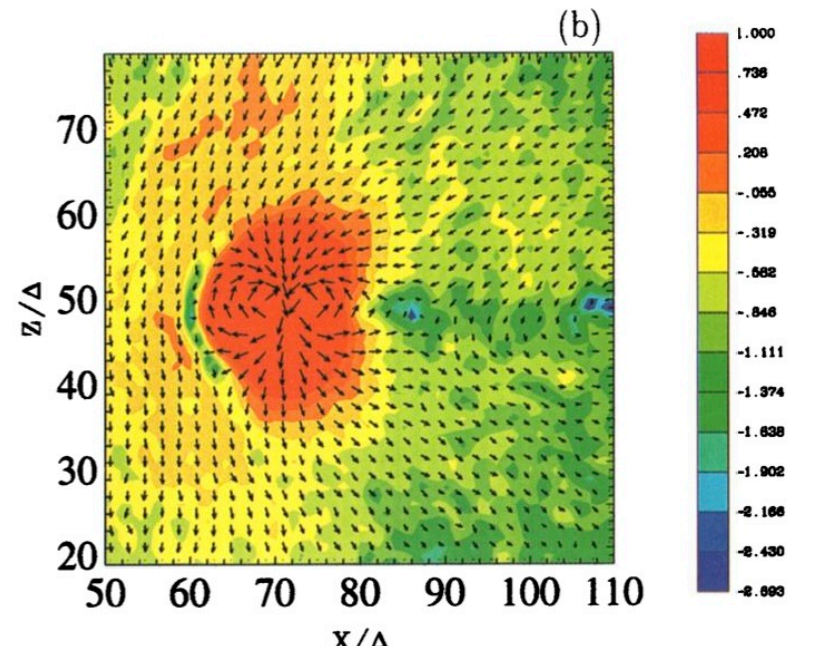
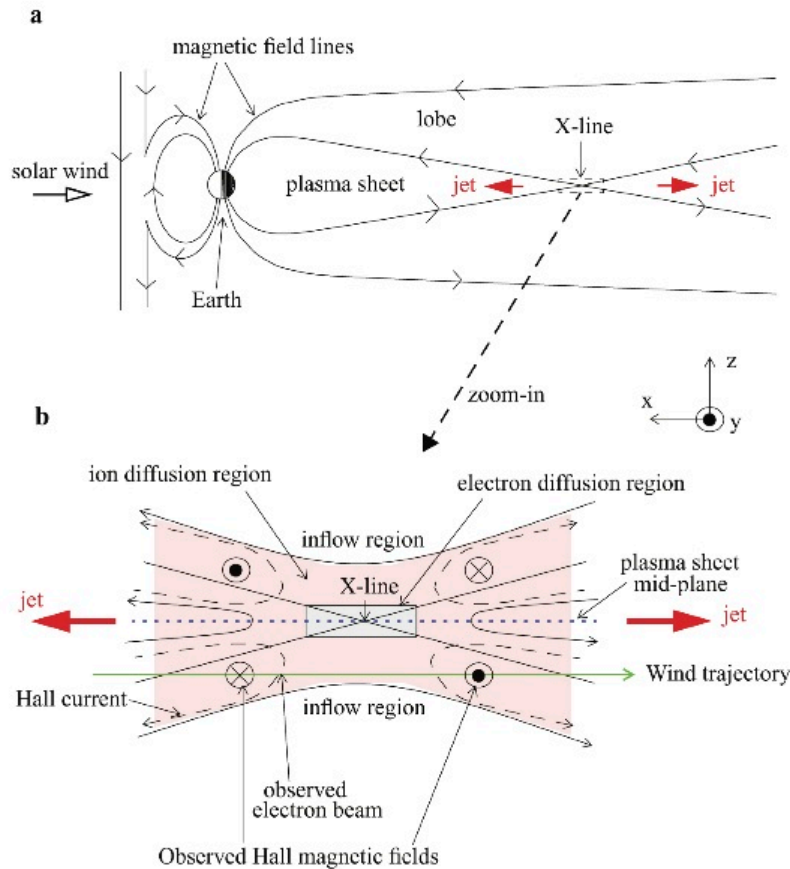
- Substorms are a consequence of reconnection rate imbalance: the nightside rate must balance dayside rate, at least on long scales ( $>1\text{h}$ ) to return flux back to the dayside.
- During a substorm, first the dayside reconnection rate exceeds the nightside rate: growth phase.
- Explosive reconnection in the nightside signals the expansion phase with auroral brightening and westward traveling surge.
- It remains an open question what triggers the expansion phase onset: 2 minute question.
- If rates balance: steady magnetospheric convection (SMC).



Russell, 1993

# Reconnection with southward IMF

## schematic reconnection



from *Report of the Workshop on Opportunities in Plasma Astrophysics*

# Space Physics According to NASA EPO

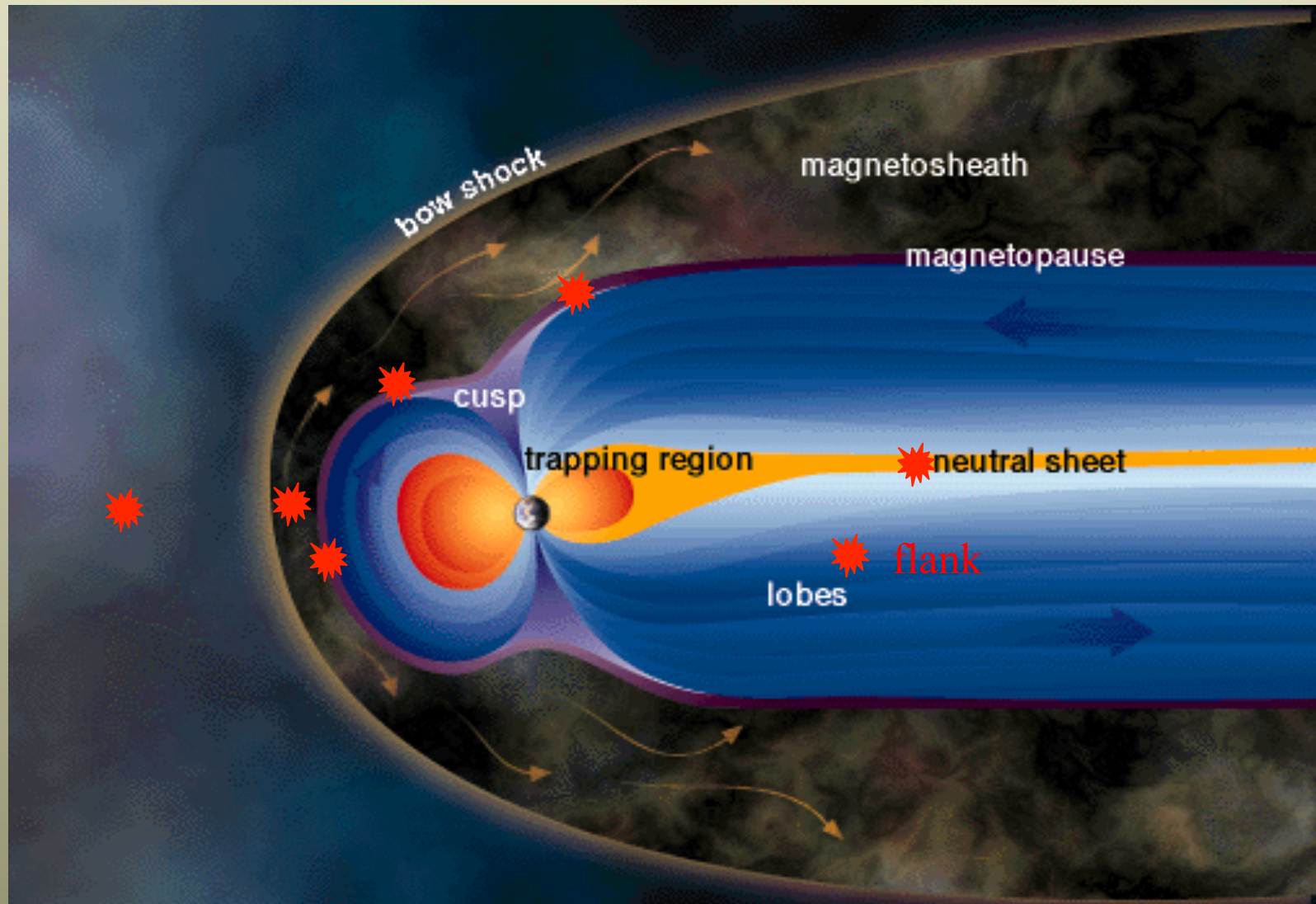
Schematic view of solar wind – magnetosphere interaction

[play SOHO5\\_CME\\_ANIM\\_EARTHA.mov](#)



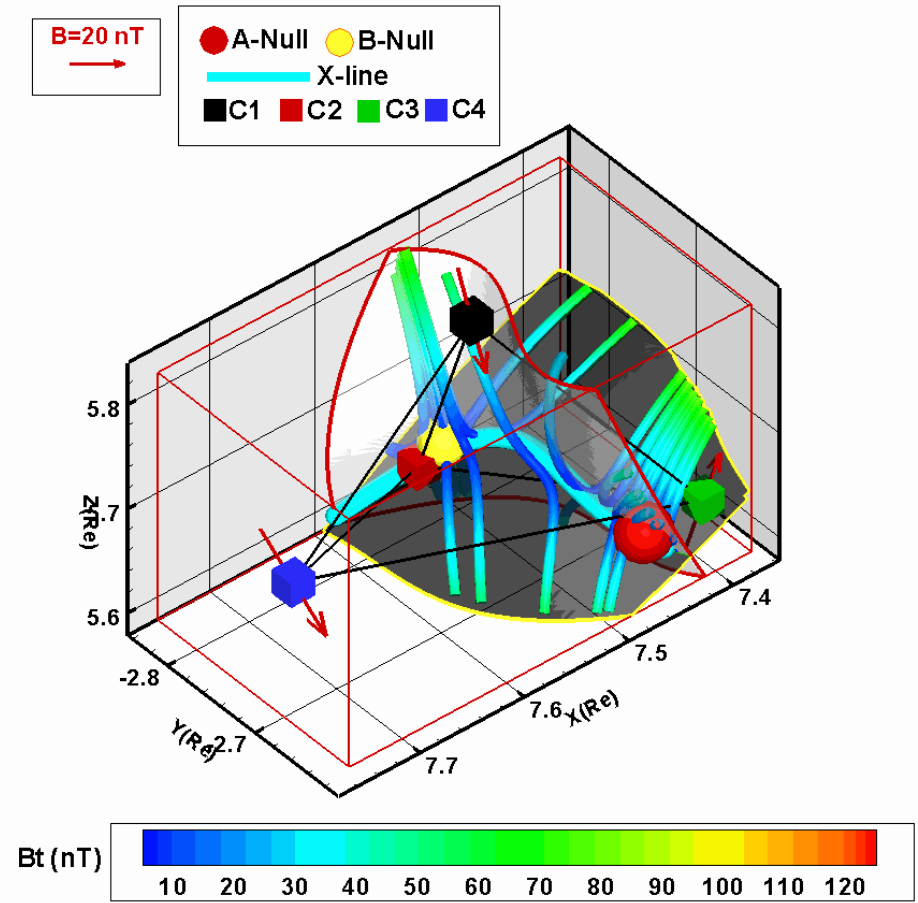
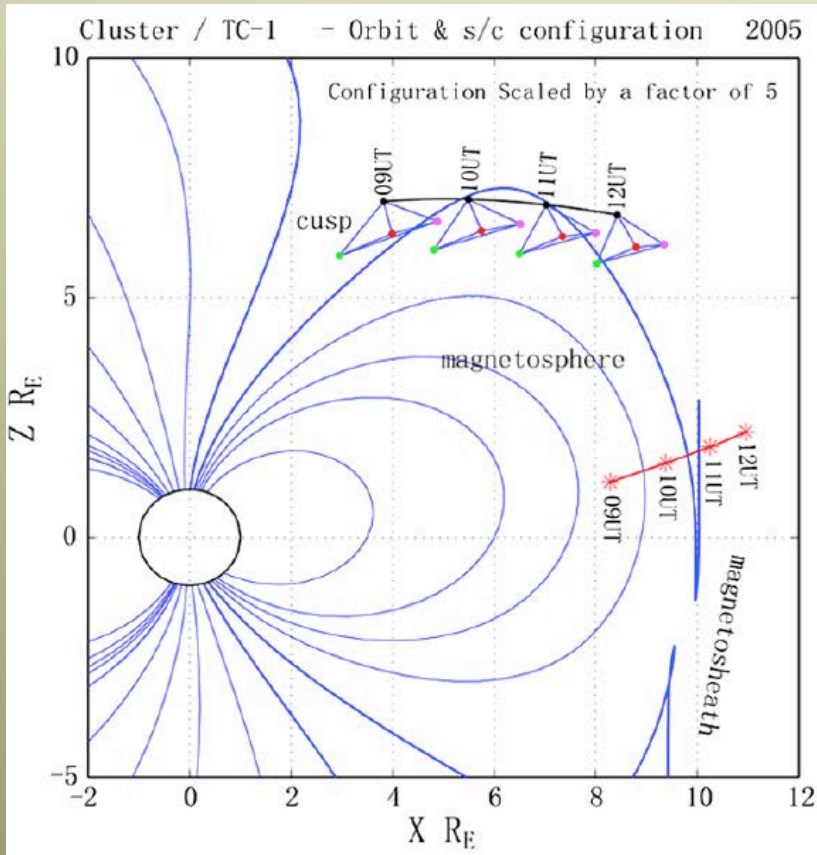
# Locations of reconnection in magnetosphere observed by Cluster

Courtesy of **C. P. Escoubet**



# B null near the cusp

## 3D Magnetic reconnection

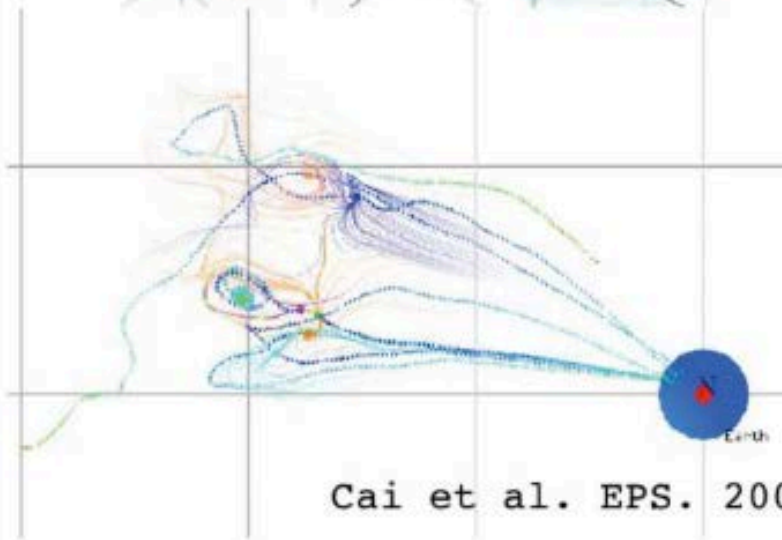
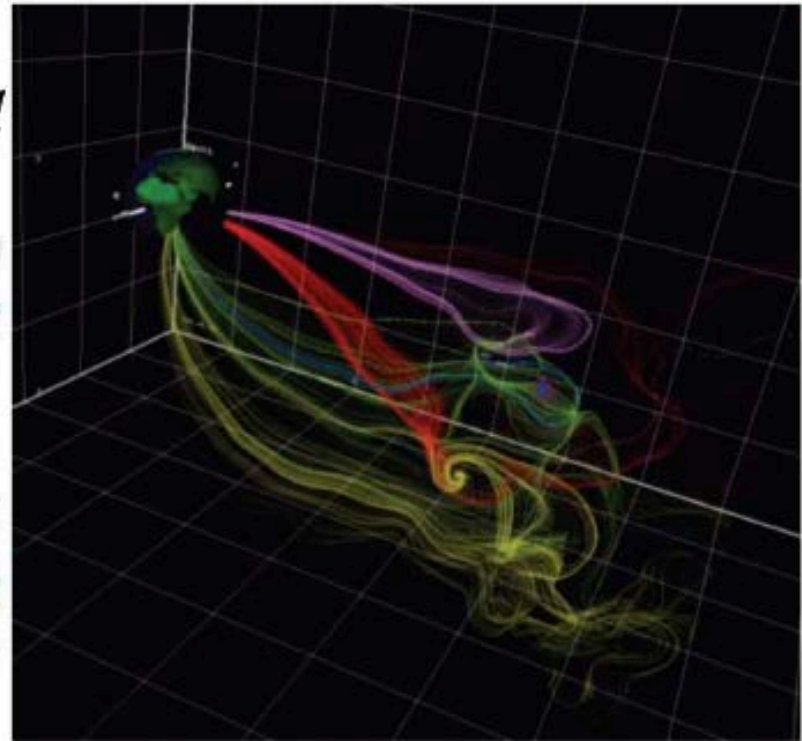
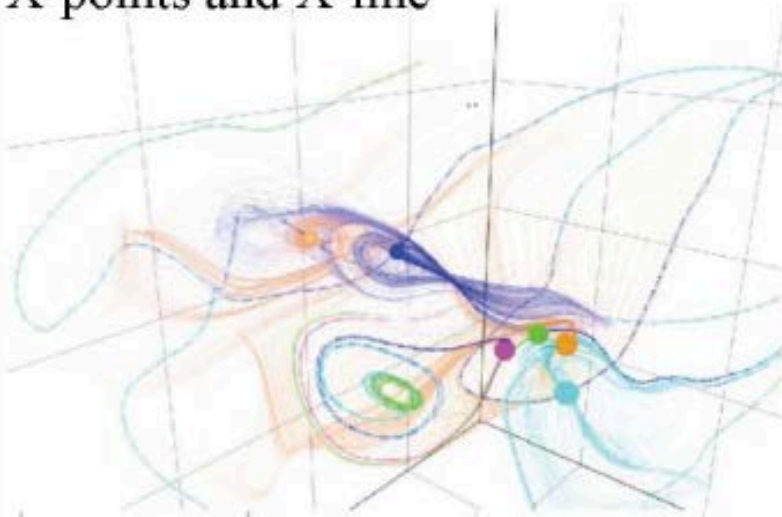


Courtesy of C. P. Escoubet

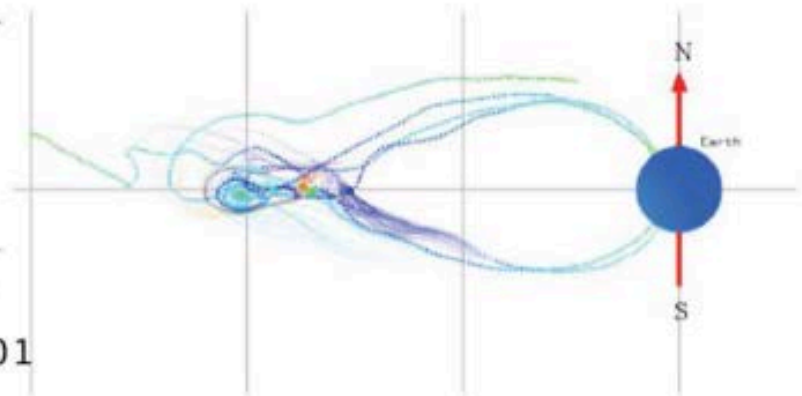
[Dunlop et al, PRL, 2009]

# *Three-dimensional topology of magnetic fields in the magnetotail*

X-points and X-line



Cai et al. EPS. 2001

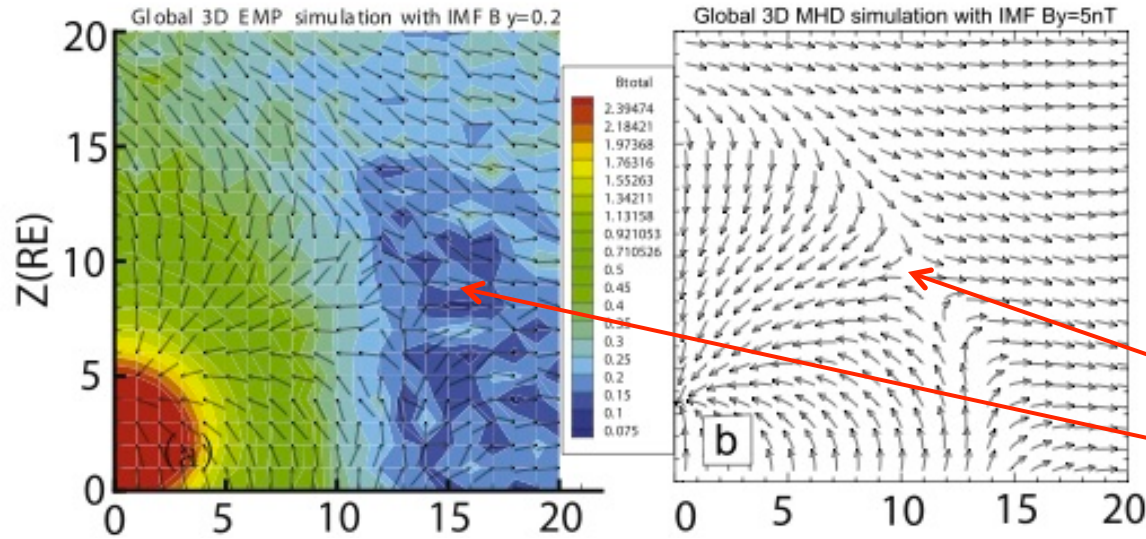


# Duskward IMF component reconnection (viewed from the Sunward)

$|B|$

$X = -5RE$

3D MHD (White et al. 1998)

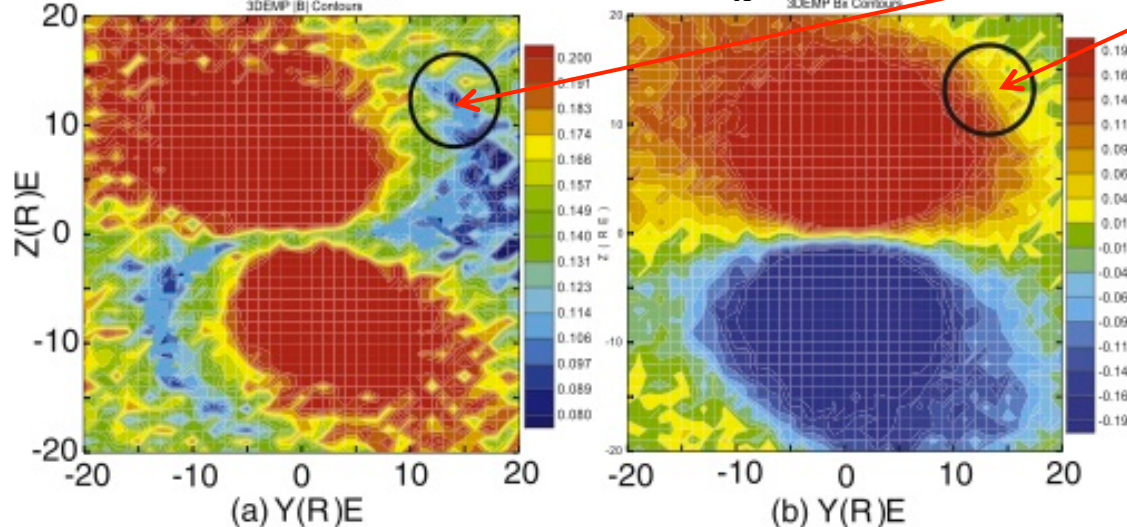


Crosstail-S is formed with duskward IMF

“sash”

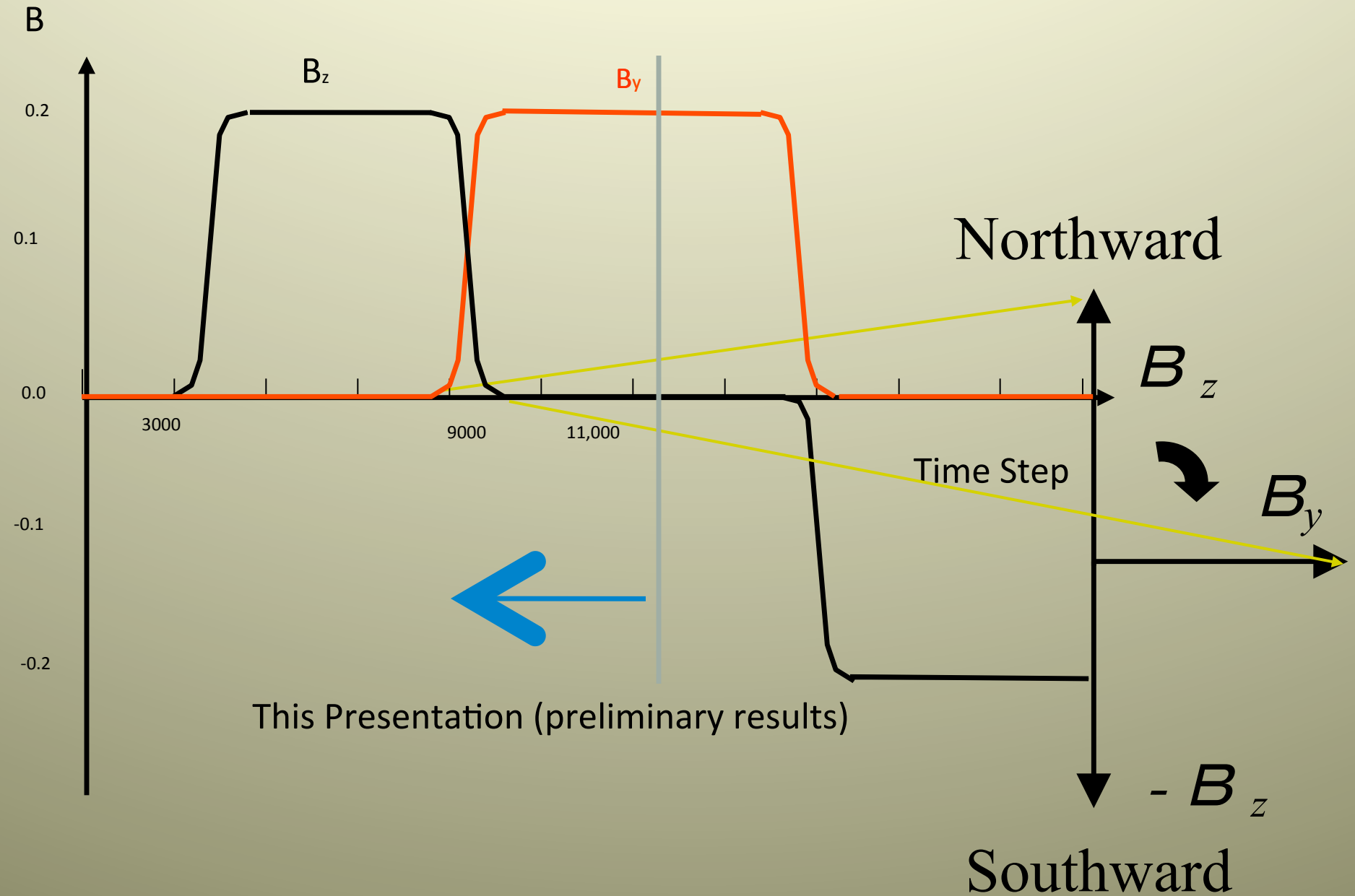
$|B|$

$X = -10RE$   $B_x$



(Cai et al. GRL, 2006)

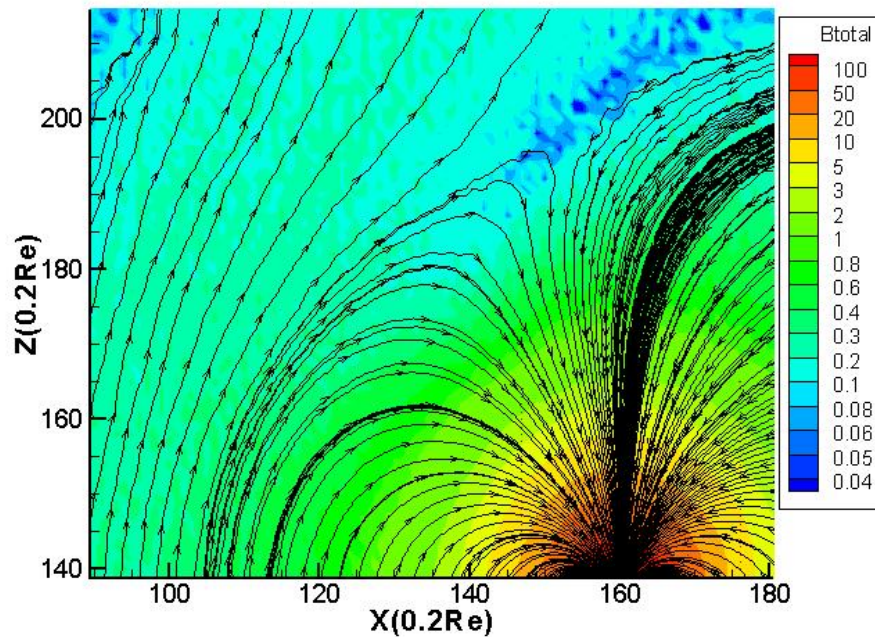
# Time Sequence of IMF Rotation from $B_z$ to $B_y$



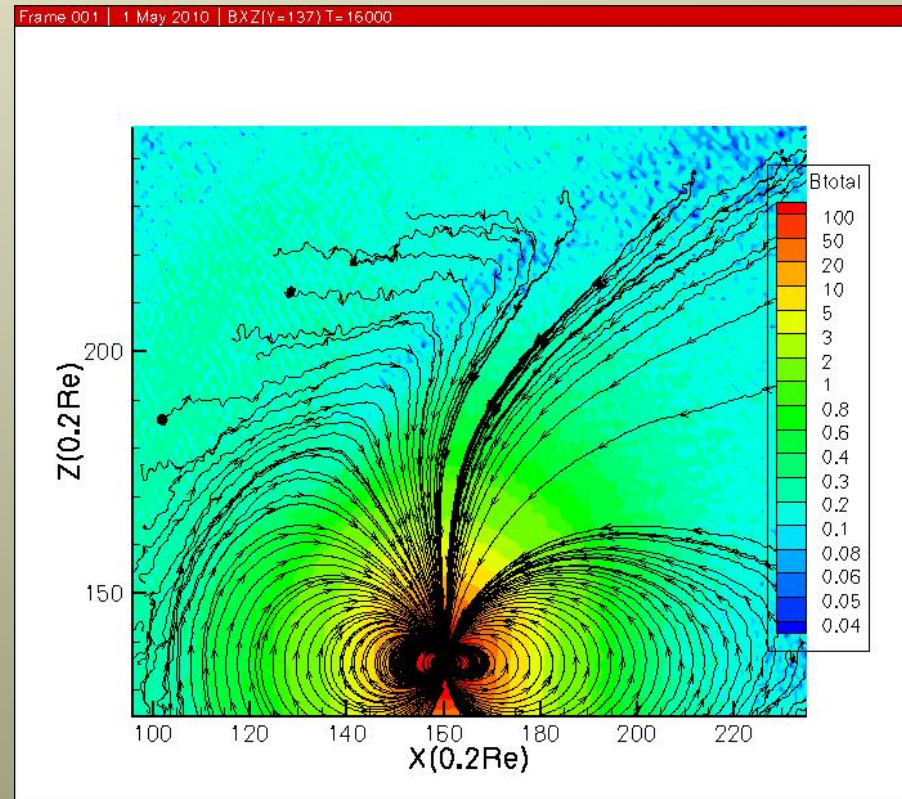
# Cusp Region (Enlarged View)

B slicing (meridian plane Z-X)

Northward IMF



Dusk-Dawn IMF



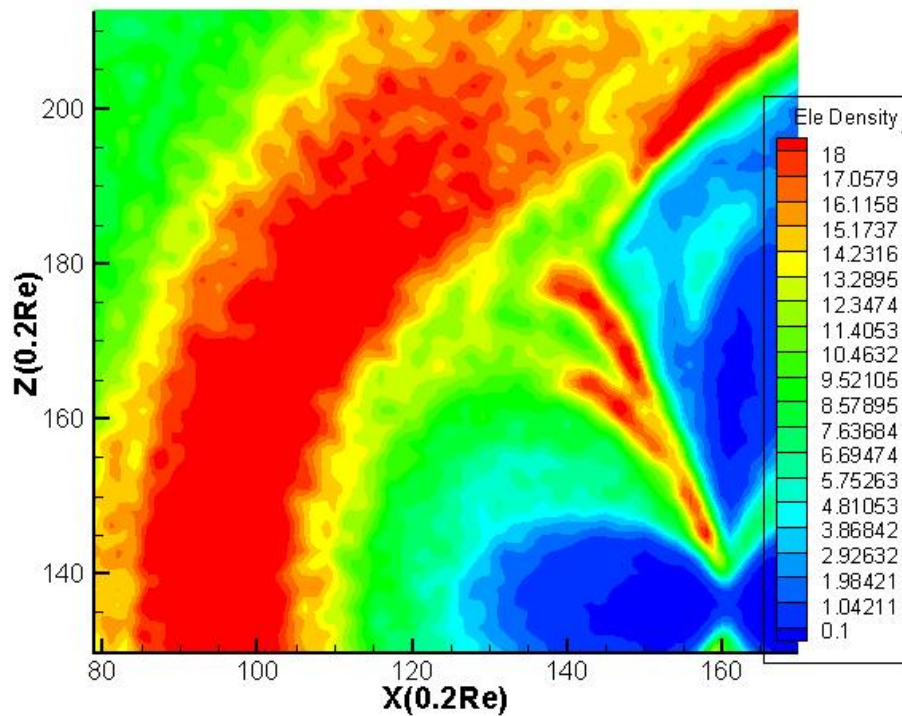
# Cusp Region (Enlarged View)

**Electron** density slicing (meridian plane Z-X)

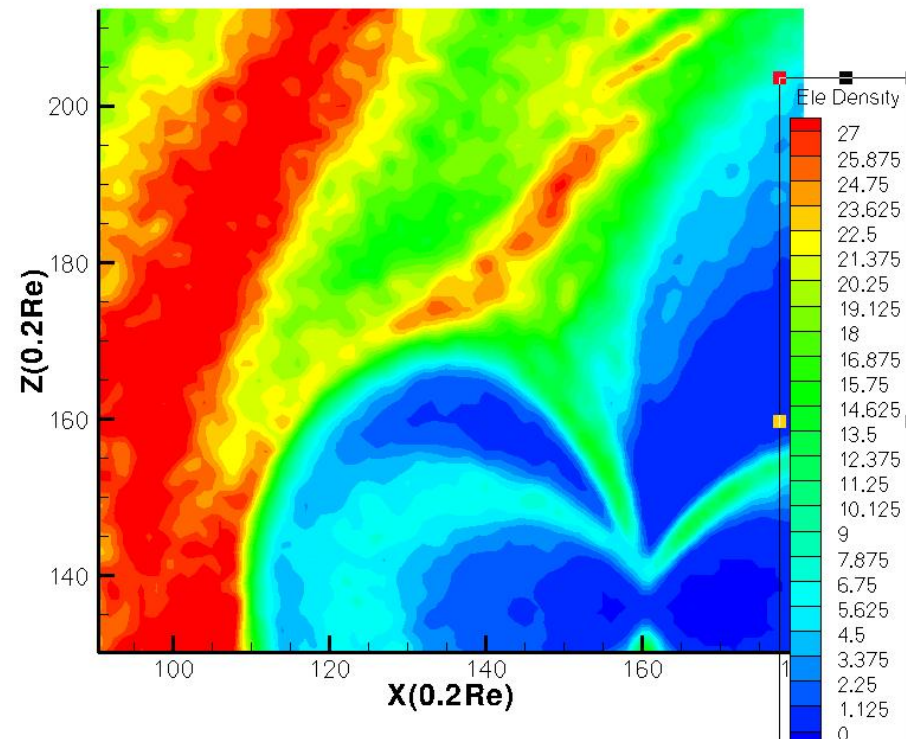
Northward IMF

Dawn-Dusk IMF

Frame 001 | 18 Dec 2009 | Elec Density (Z=137) T=7500



Frame 001 | 4 May 2010 | Elec Density (Y=137) T=16000

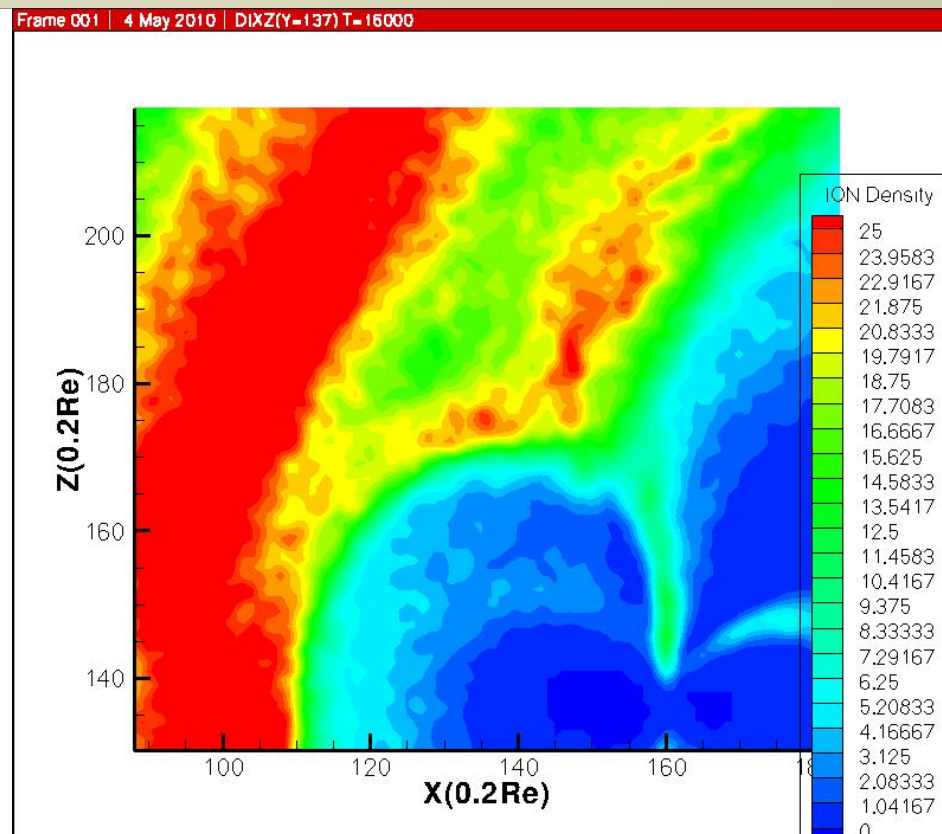
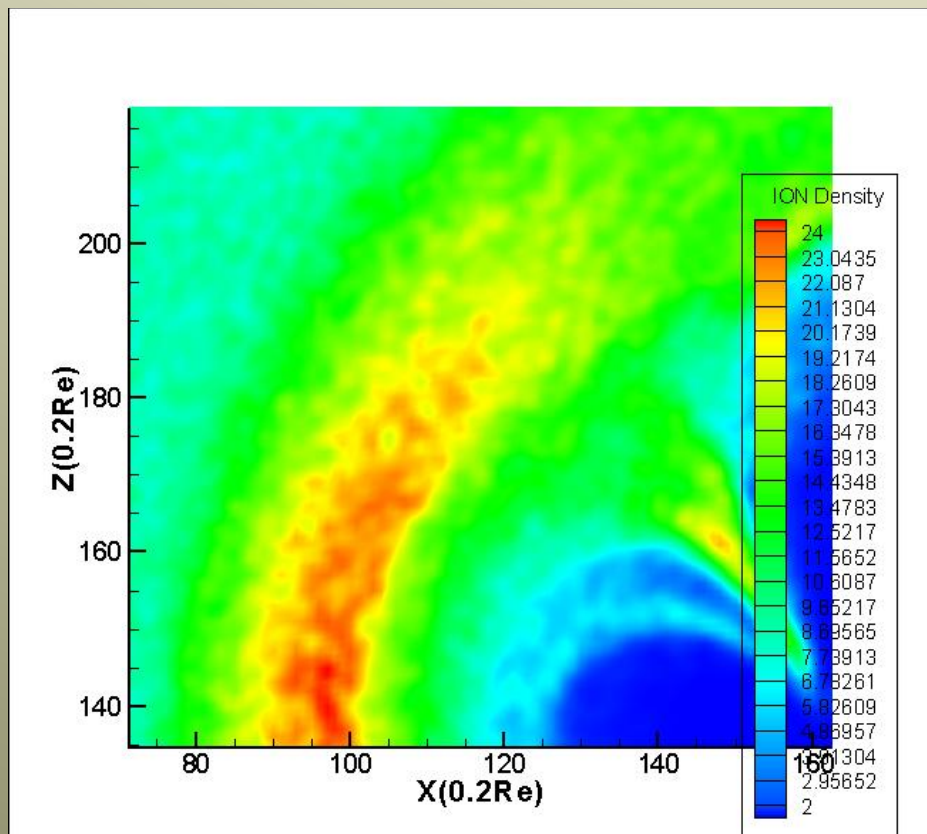


# Cusp Region (Enlarged View)

Ion density slicing (meridian plane Z-X)

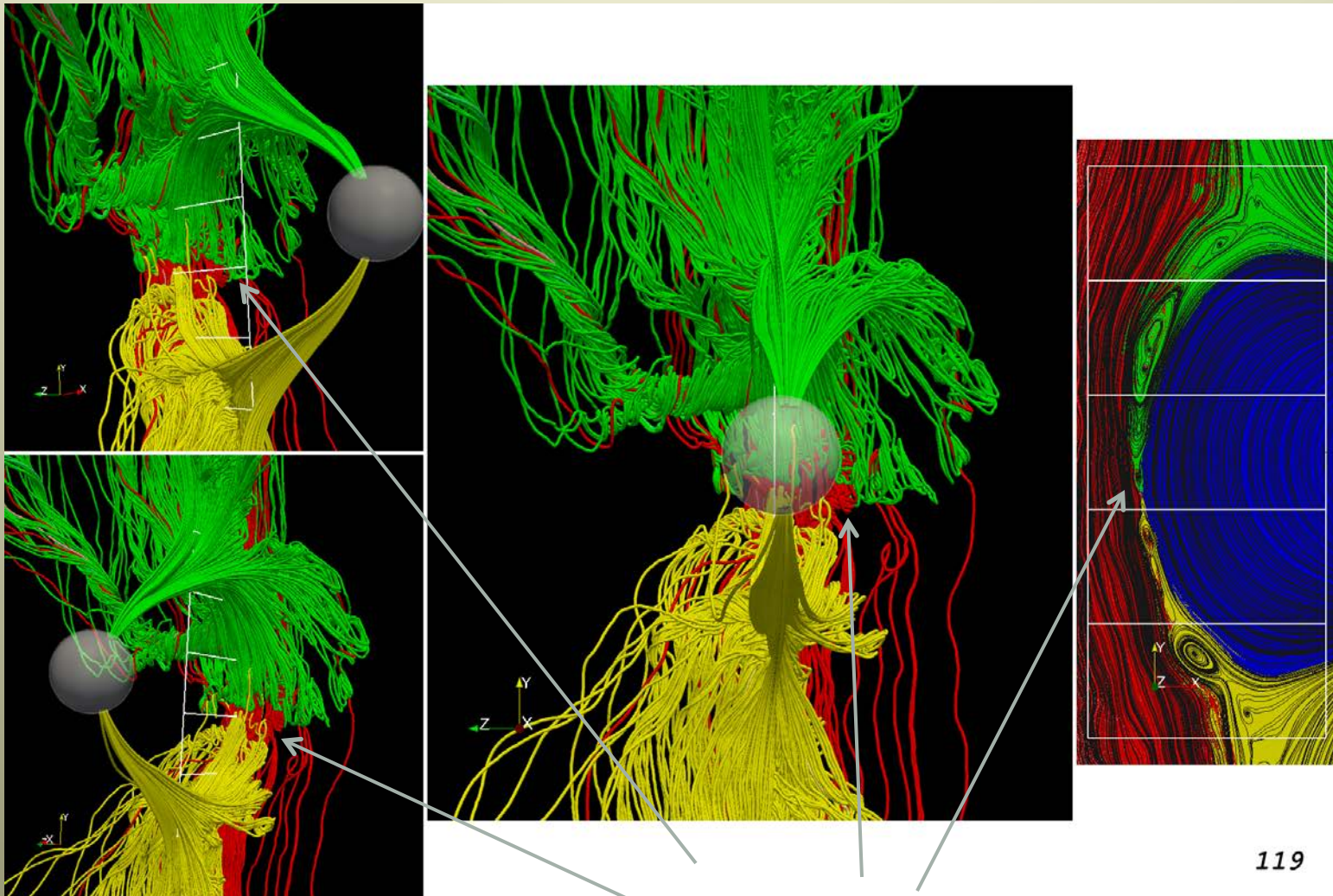
Northward IMF

Dawn-Dusk IMF



# Peta-Scale 3D Global Hybrid Simulations

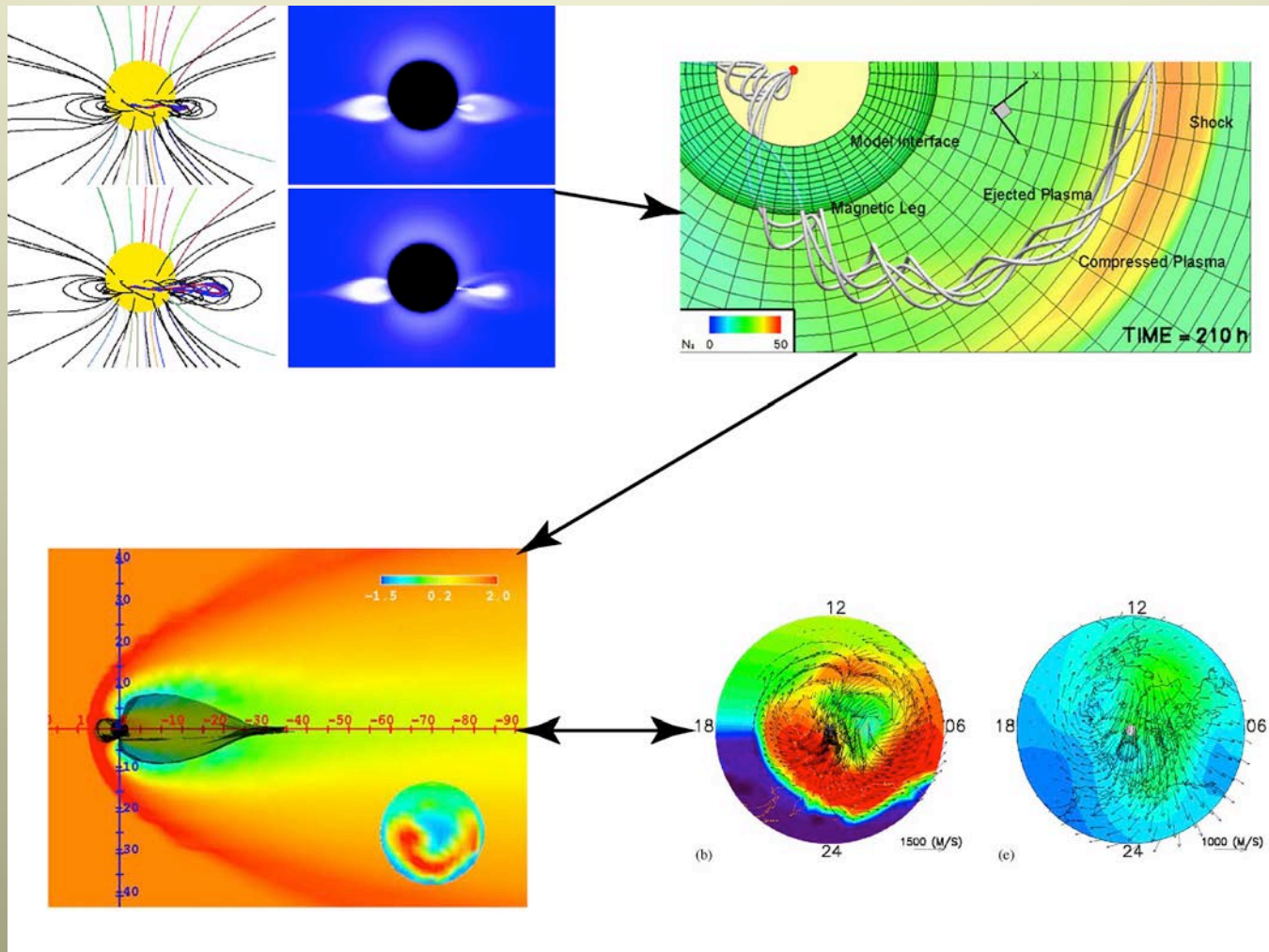
(Karimabadi, et al., GRL, to be submitted, 2010)



119

reconnection (courtesy of H. Karimabadi)

# Coupled-Model Simulation from Sun to Earth



# Astrophysical Jets

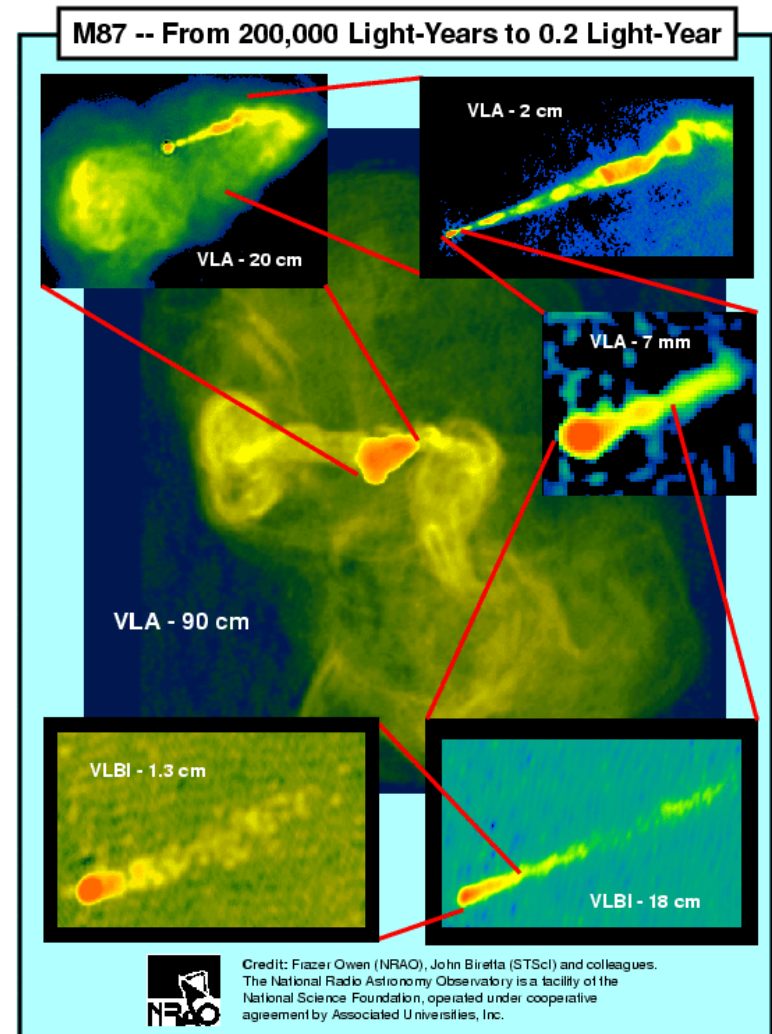
⊙ *Astrophysical jets: outflow of highly collimated plasma*

- ⊙ Microquasars, Active Galactic Nuclei, Gamma-Ray Bursts, **Jet velocity  $\sim c$ , Relativistic Jets.**
- ⊙ Generic systems: Compact object (White Dwarf, Neutron Star, Black Hole) + Accretion Disk

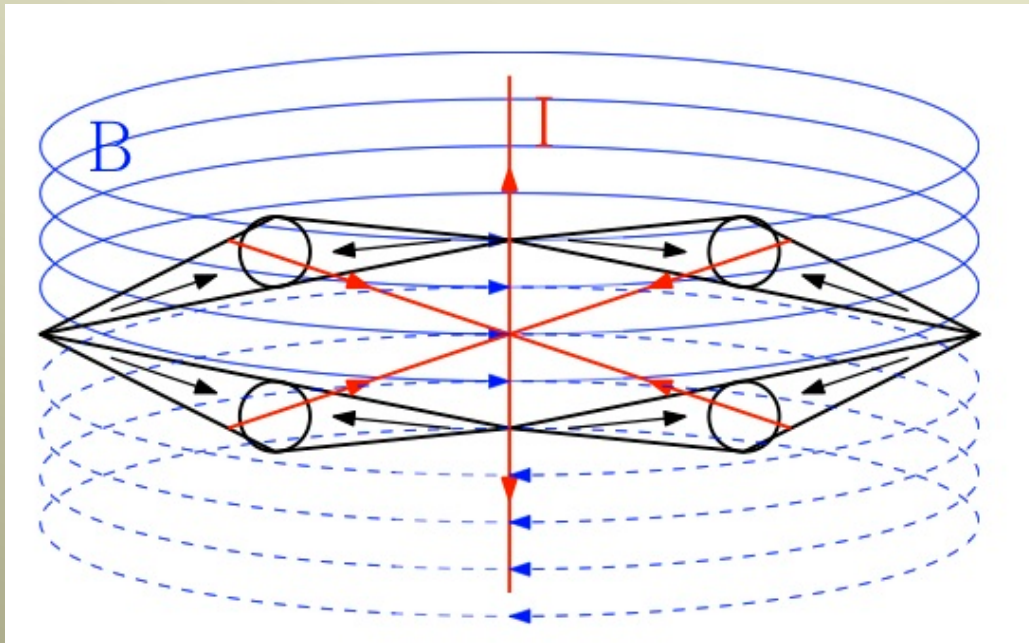
⊙ *Key Problems of Astrophysical Jets*

- ⊙ Acceleration mechanism and radiation processes
- ⊙ Collimation
- ⊙ Long term stability

M87



# Reconnection-Powered Minijets in Blazars



Schematic representation of a toroidal current sheet at the boundary of two magnetic domains of opposite polarity, showing orientations of magnetic fields (*blue*), currents (*red*) and minijet flows (*black arrows*) from X-points to O-points.

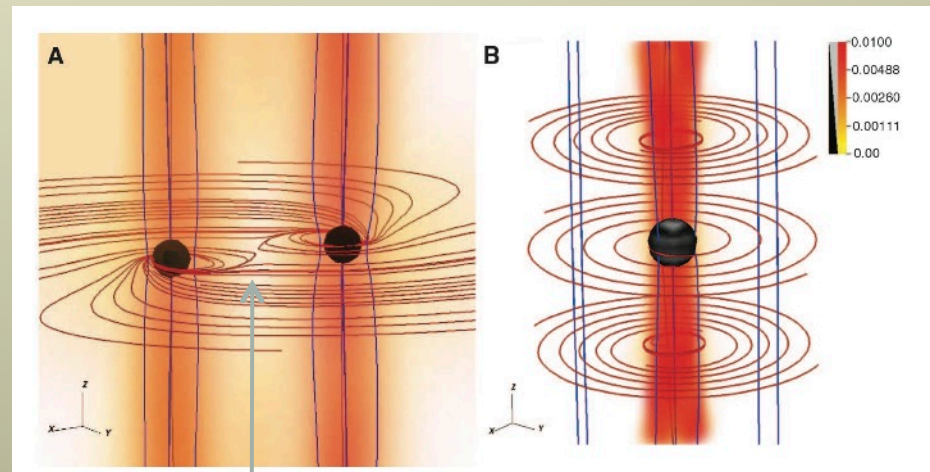
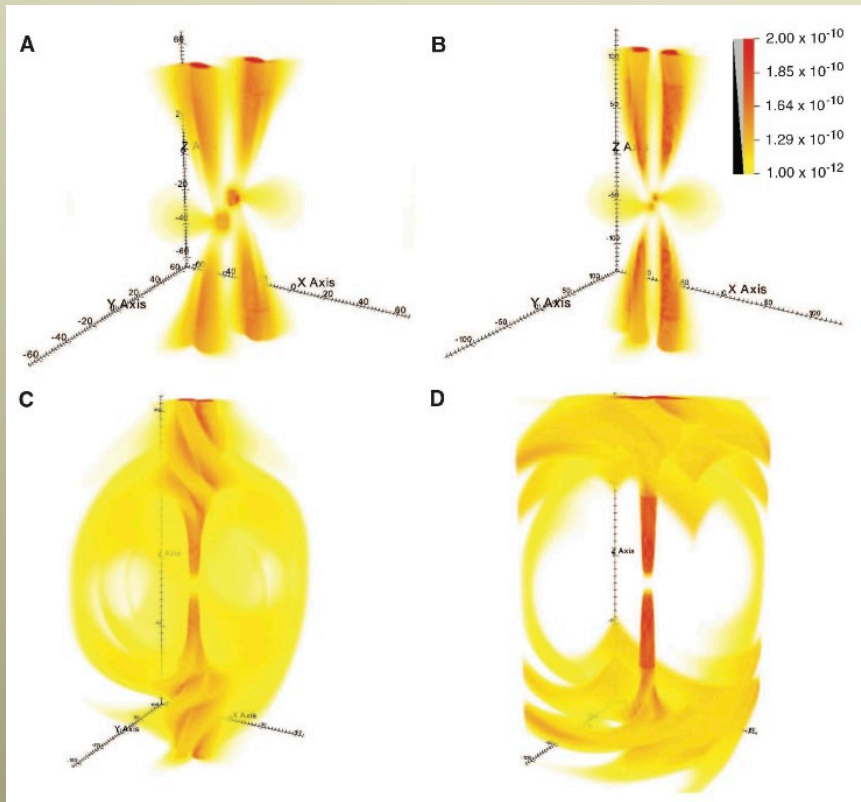
(Nalewajko et al. MNRAS, 413, 333, 2011)

# *Recent Work for Relativistic Jets*

- ⊗ Investigate **the role of magnetic fields in relativistic jets** against three key problems
  - ⊗ Jet formation
  - ⊗ Jet acceleration and radiation process
    - ⊗ **Acceleration of particles to very high energy**
  - ⊗ Jet stability
    - ⊗ **Kelvin-Helmholtz instability**
    - ⊗ **Current-Driven instability**
  
- ⊗ **Recent research topics**
  - ⊗ Development of 3D general relativistic MHD (GRMHD) code “RAISHIN”
  - ⊗ GRMHD simulations of jet formation and radiation from Black Hole magnetosphere
  - ⊗ A relativistic MHD boost mechanism for relativistic jets
  - ⊗ Stability analysis of magnetized spine-sheath relativistic jets
  - ⊗ **Particle-In-Cell (PIC) simulations of relativistic jets**

**play 3Dprej5b\_1.mov for kink instability**

# Reconnection during merging black hole binary?

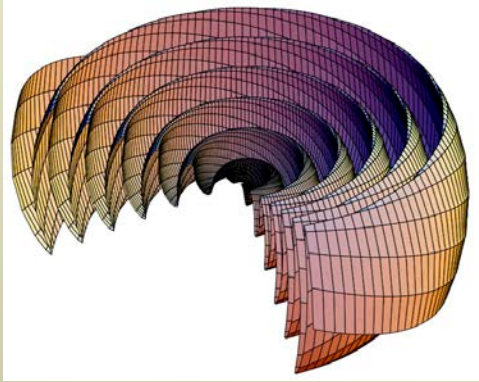


reconnection?

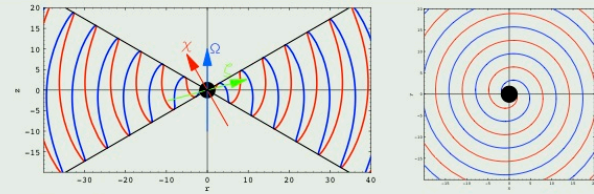
(Palenzuela, Lehner, & Liebling, Science, 329, 927, 2010)

# PIC simulation

[play combinedmovie.mov](#)

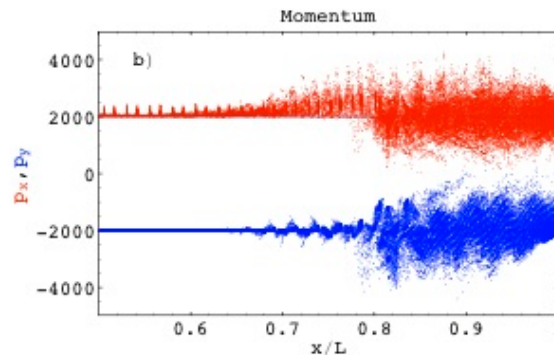
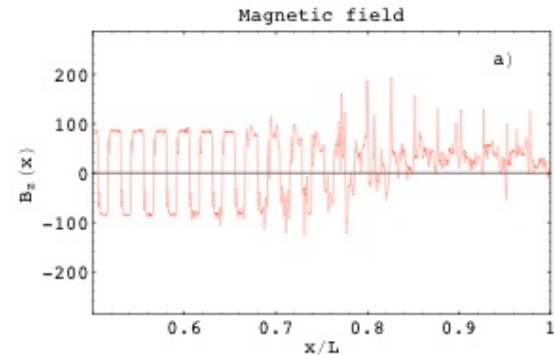
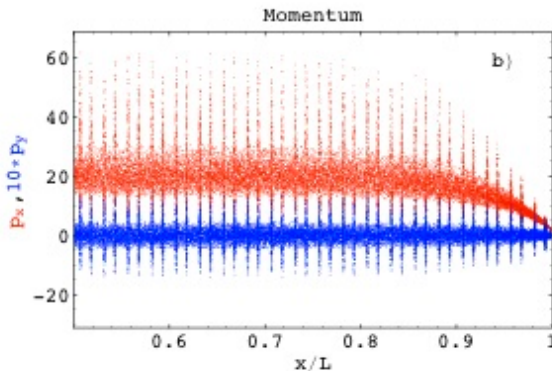
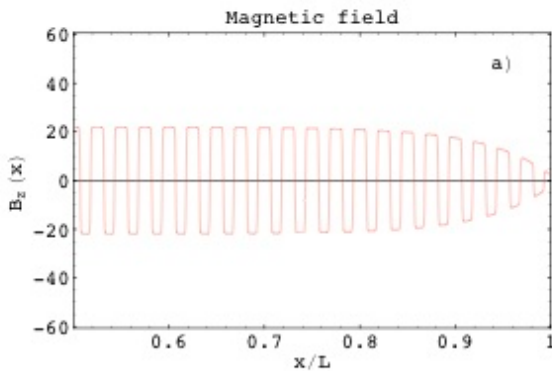


Asymptotic MHD solution : oblique rotator (Bogovalov 1999)

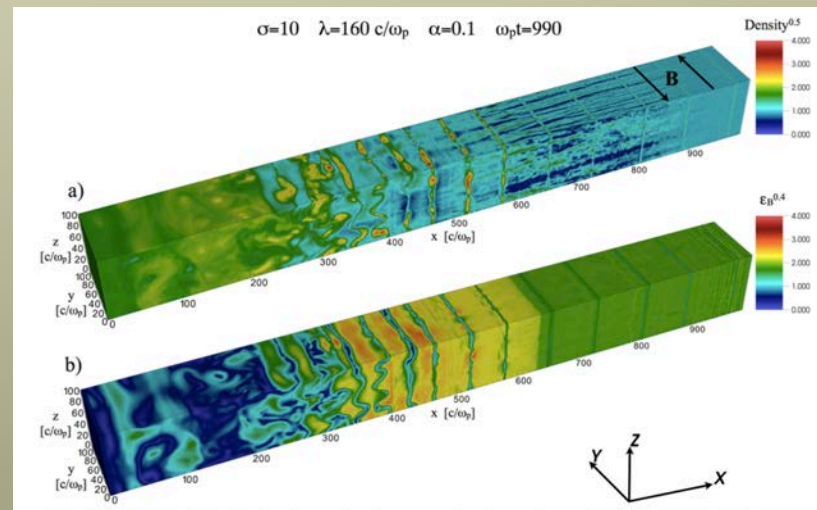
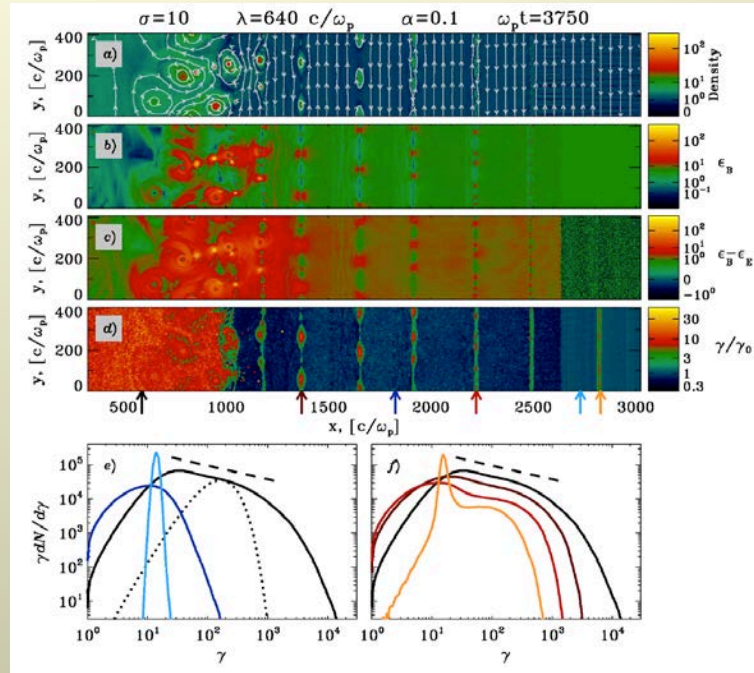
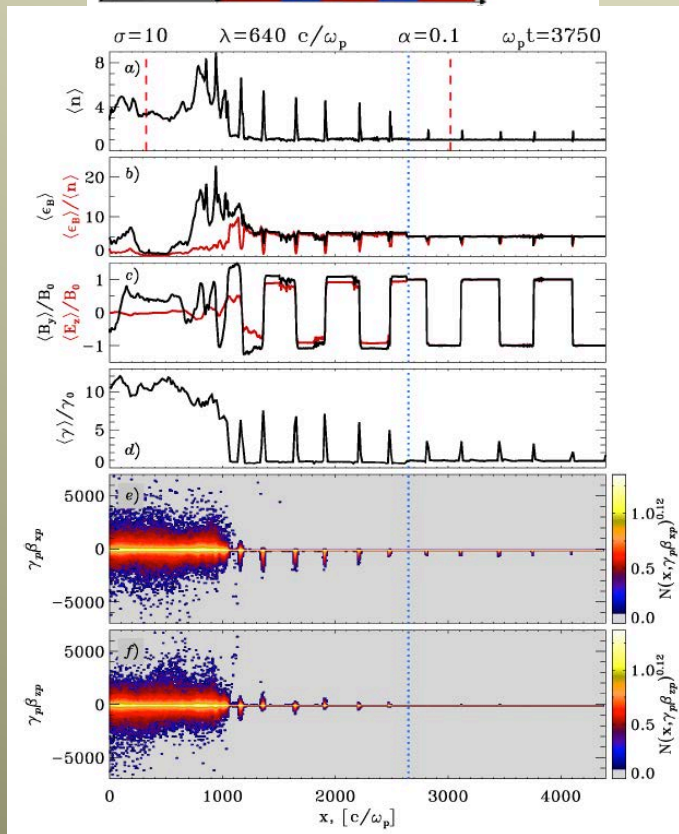
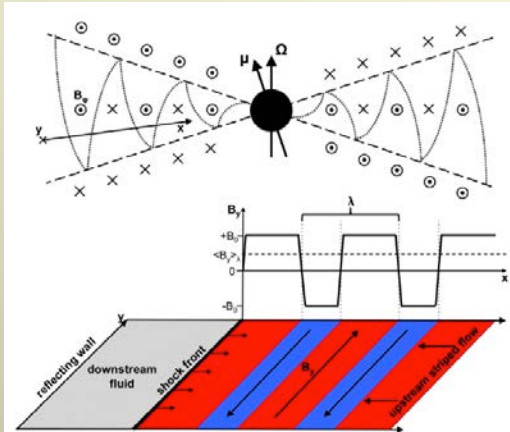


- $\Omega$  : rotation axis ;
- $\chi$  : inclination of magnetic axis ;
- $\zeta$  : inclination of line of sight.

negligible dissipation with  $\sigma = 3, \Gamma = 20$       dissipation with  $\sigma = 45, \Gamma = 20$

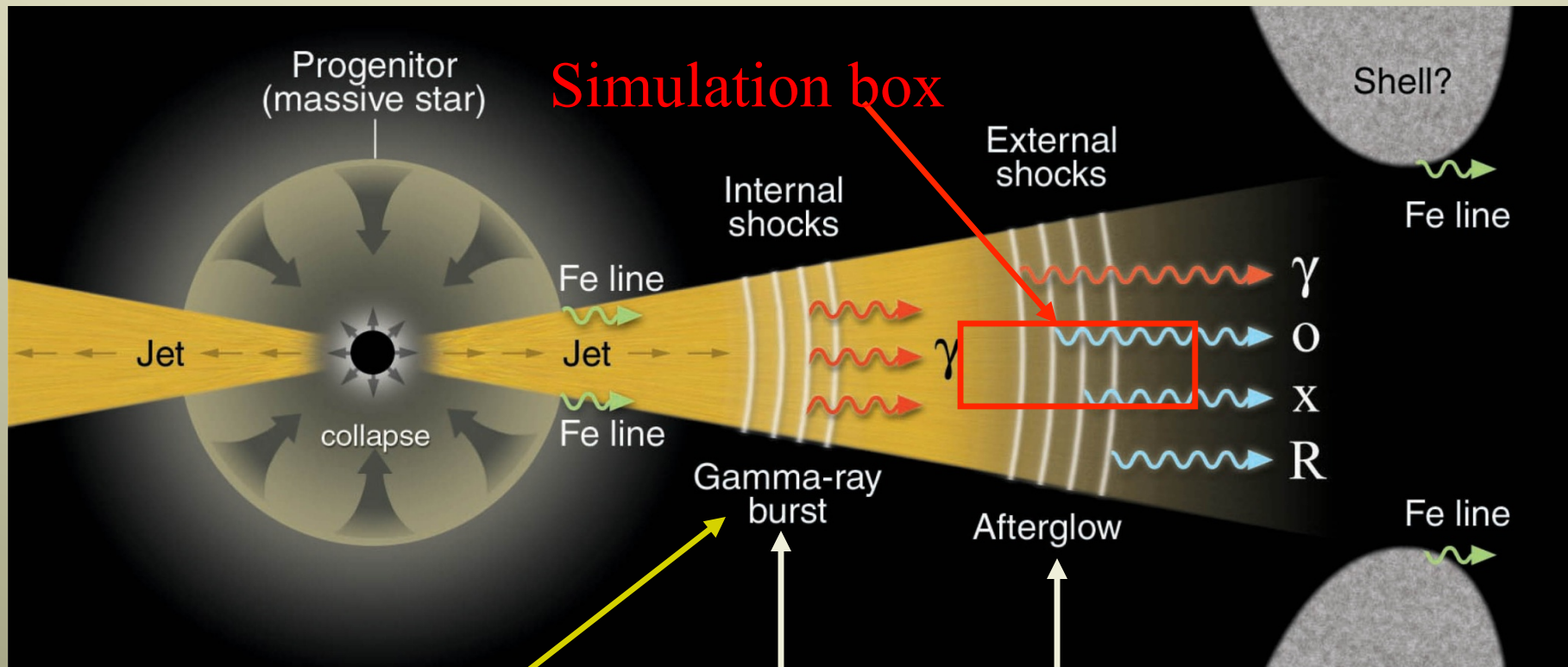


# 2-D Striped wind simulation



# *Schematic GRB from a massive stellar progenitor*

(Meszaros, Science 2001)



Prompt emission

Gamma-ray burst

Afterglow

Polarization ?

Accelerated particles emit waves at shocks

### 3-D isosurfaces of z-component of current $J_z$ for narrow jet ( $\gamma v_{||}=12.57$ )

electron-ion ambient

$$t = 59.8\omega_e^{-1}$$

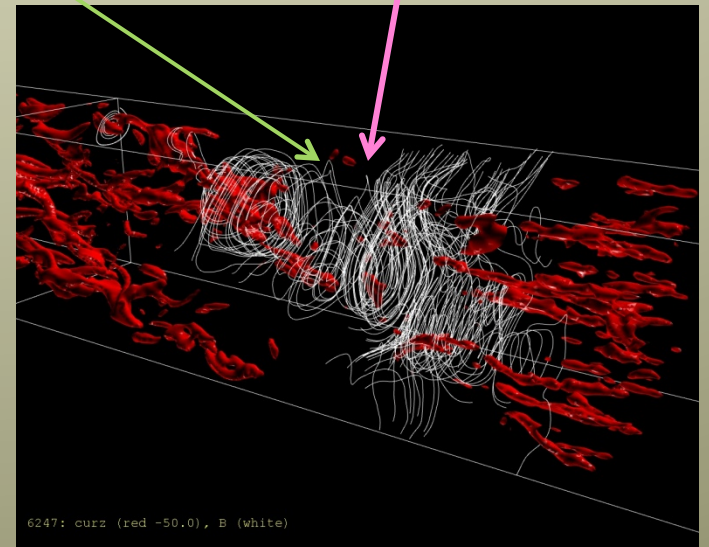
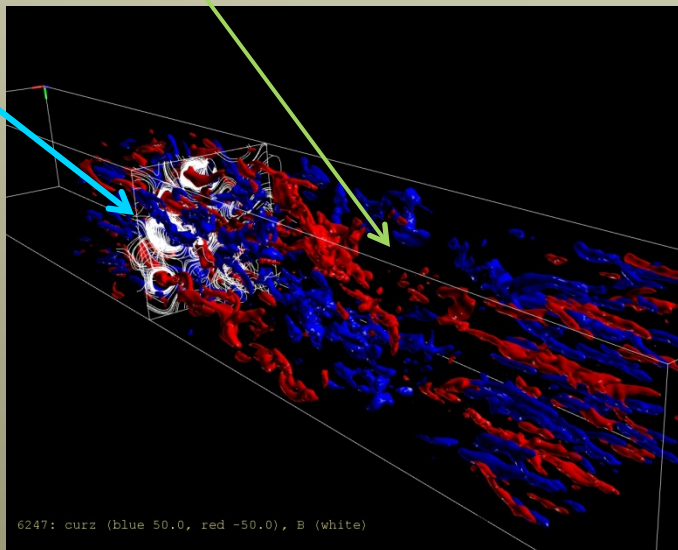
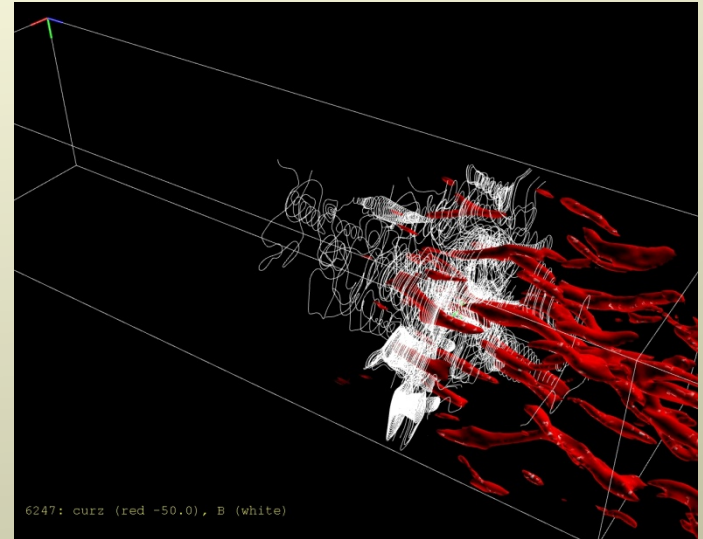
$-J_z$  (red),  $+J_z$  (blue), magnetic field lines (white)

*Particle acceleration due to the local reconnections during merging current filaments at the nonlinear stage*

*thin filaments*

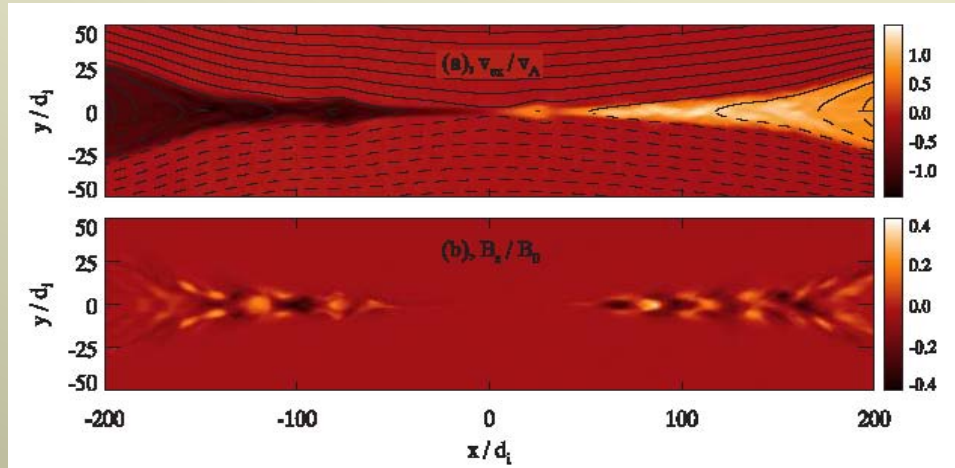
play apf62jzB.avi

*merged filaments*



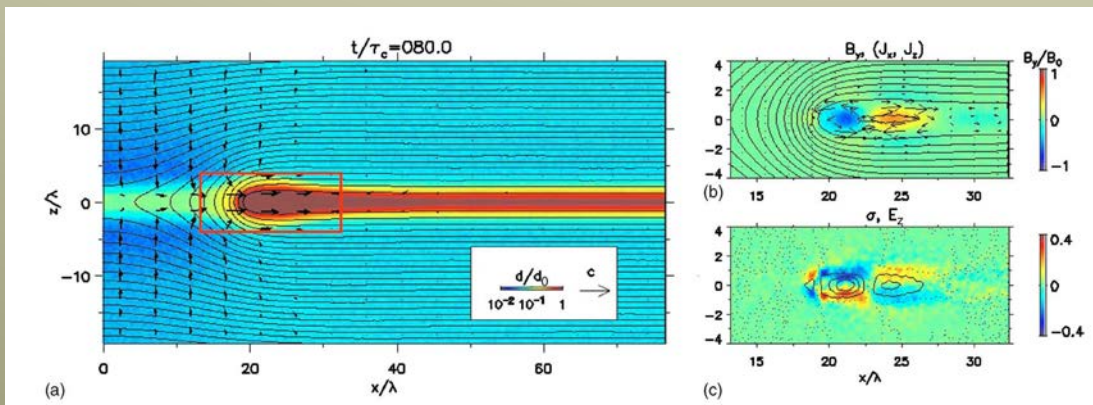
# Weibel instability in reconnections

Electron beam excite the Weibel instability



nonrelativistic reconnection

(Swisdak, Liu, & Drake ApJ, 2008)



relativistic reconnection

(Zenitania & Hesse, PoP, 2008)

Cracow 2008 conference presentations

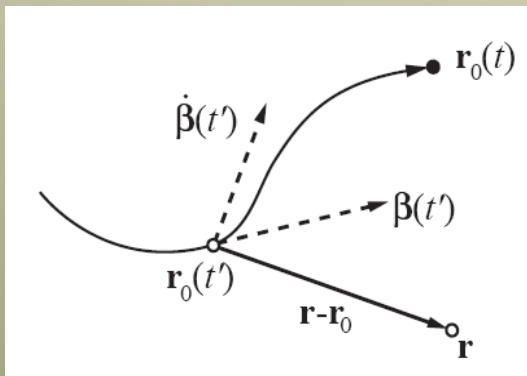
<http://www.oa.uj.edu.pl/cracow2008/Program.html>

## *Radiation from particles in collisionless shock*

To obtain a spectrum, “just” integrate:

$$\frac{d^2W}{d\Omega d\omega} = \frac{\mu_0 c q^2}{16\pi^3} \left| \int_{-\infty}^{\infty} \frac{\mathbf{n} \times [(\mathbf{n} - \boldsymbol{\beta}) \times \dot{\boldsymbol{\beta}}]}{(1 - \boldsymbol{\beta} \cdot \mathbf{n})^2} e^{i\omega(t' - \mathbf{n} \cdot \mathbf{r}_0(t')/c)} dt' \right|^2$$

where  $\mathbf{r}_0$  is the position,  $\boldsymbol{\beta}$  the velocity and  $\dot{\boldsymbol{\beta}}$  the acceleration

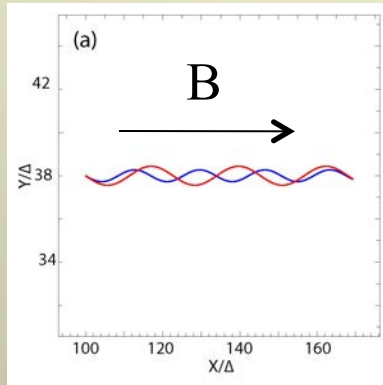


*New approach:* Calculate radiation from integrating position, velocity, and acceleration of ensemble of particles (electrons and positrons)

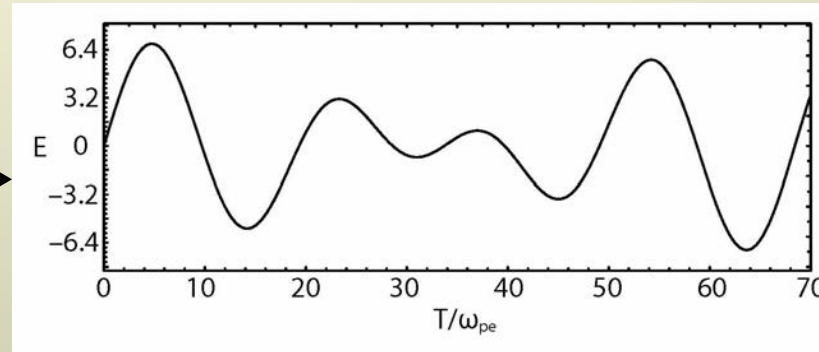
Hededal, Thesis 2005 (astro-ph/0506559)  
Nishikawa et al. 2008 (astro-ph/0802.2558)  
Sironi & Spitkovsky, 2009, ApJ  
Martins et al. 2009, Proc. of SPIE Vol. 7359  
Nishikawa et al. 2011, ASR

# *Synchrotron radiation from propagating electrons in a uniform magnetic field*

electron trajectories



radiation electric field observed at long distance

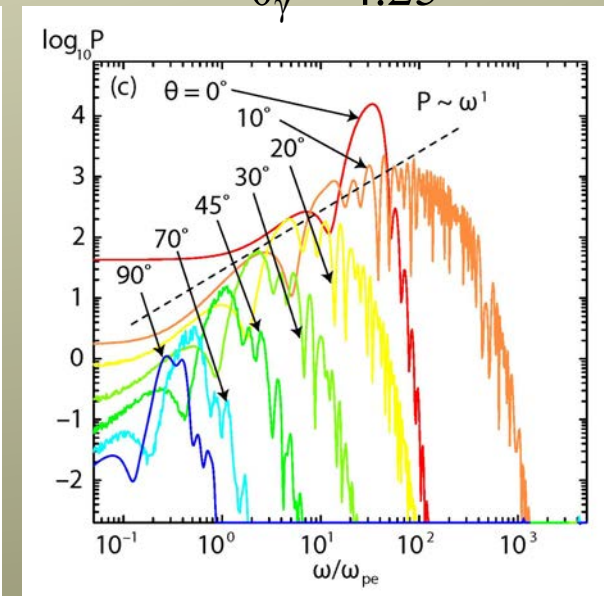
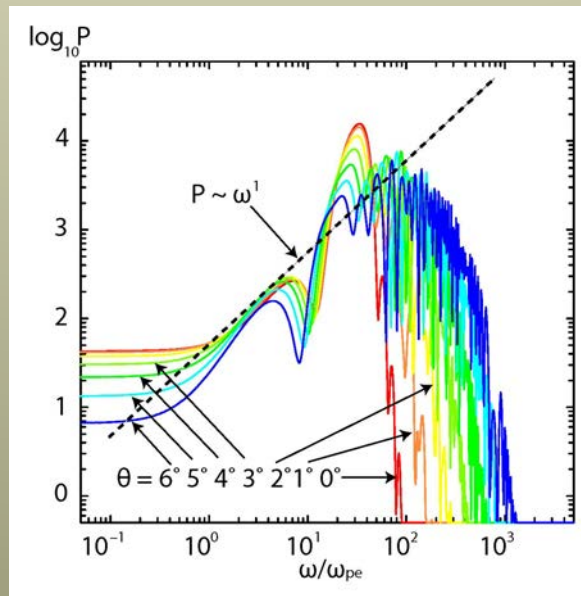
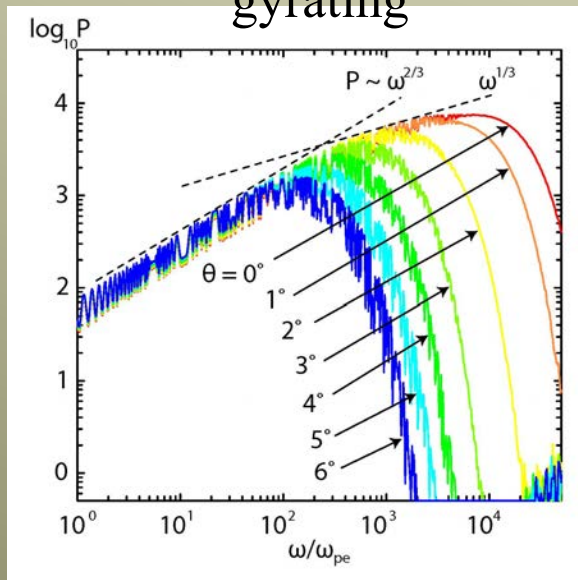


observer

spectra with different viewing angles (helical)

$\theta_\gamma = 4.25^\circ$

gyrating

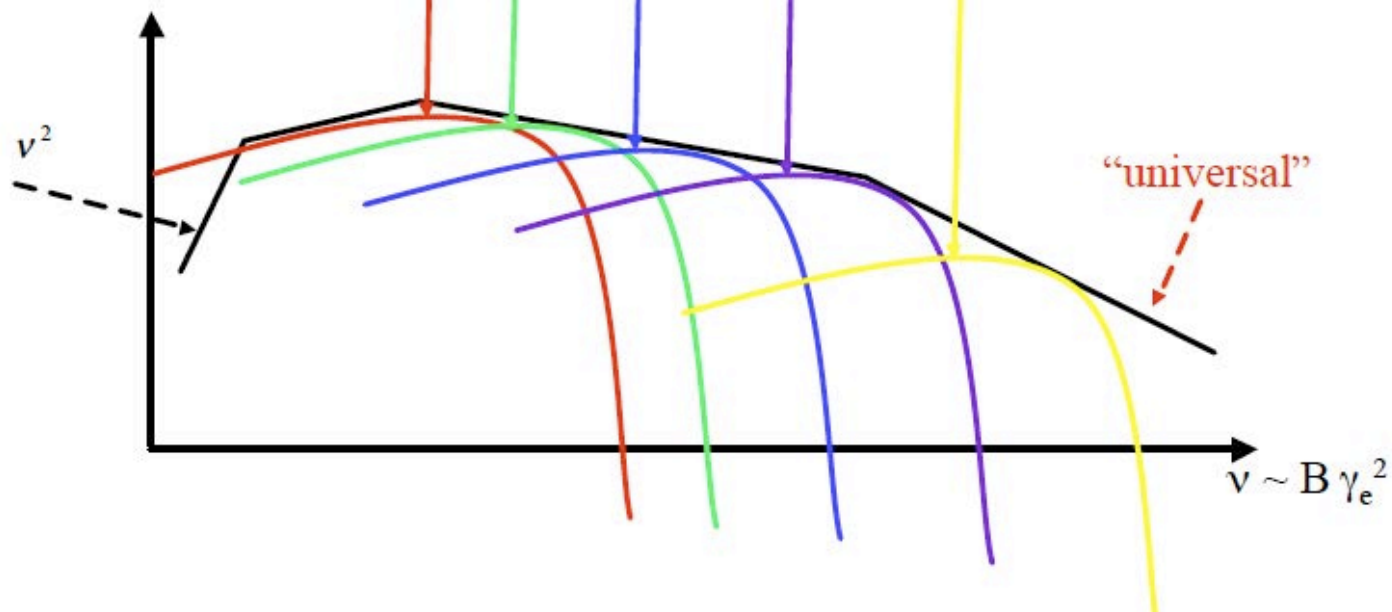
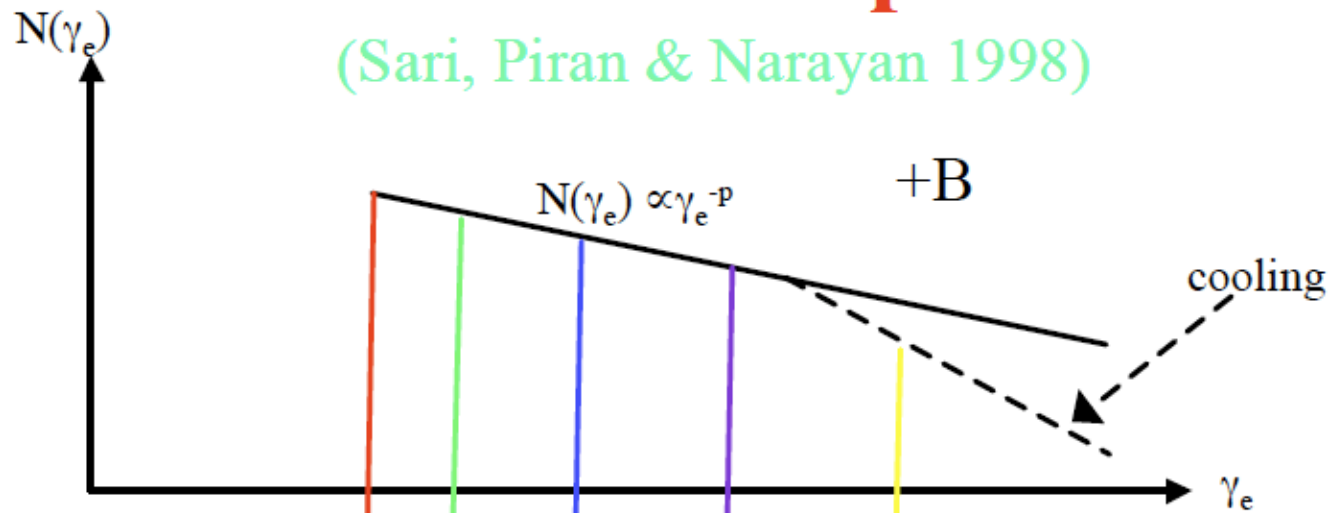


# Synchrotron Emission: radiation from accelerated

adapted by Kobayashi

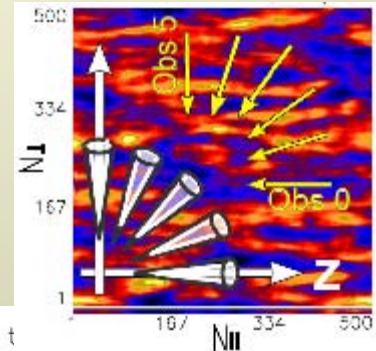
## Theoretical Spectra

(Sari, Piran & Narayan 1998)



# Importance of Synchrotron radiation calculated in 3-D system

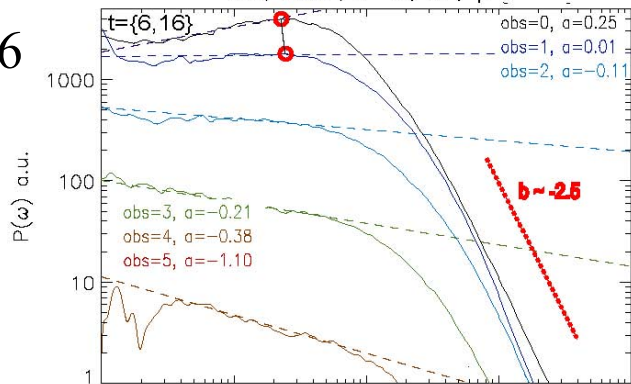
$\gamma = 6$ ,  $P^+ e^-$  counter-streaming jet, no shock generated



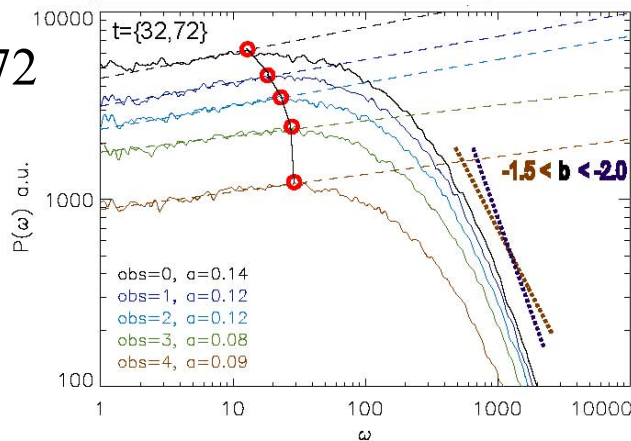
3D

3D,  $500^3$ ,  $\Gamma=6$ ,  $6^h$ ,  $p^+e^-$

$6 < t < 16$



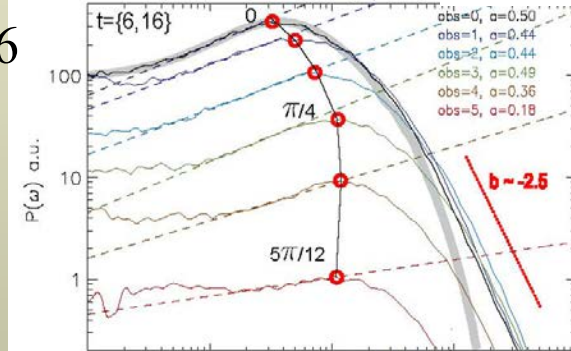
$32 < t < 72$



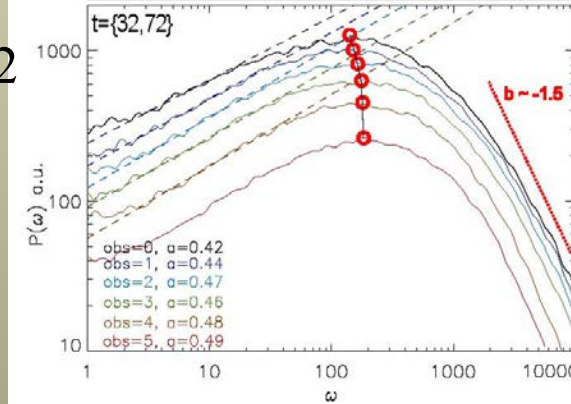
2D

2D,  $6000^2$ ,  $\Gamma=6$ ,  $6^h$ ,  $p^+e^-$ ,  $t$

$6 < t < 16$

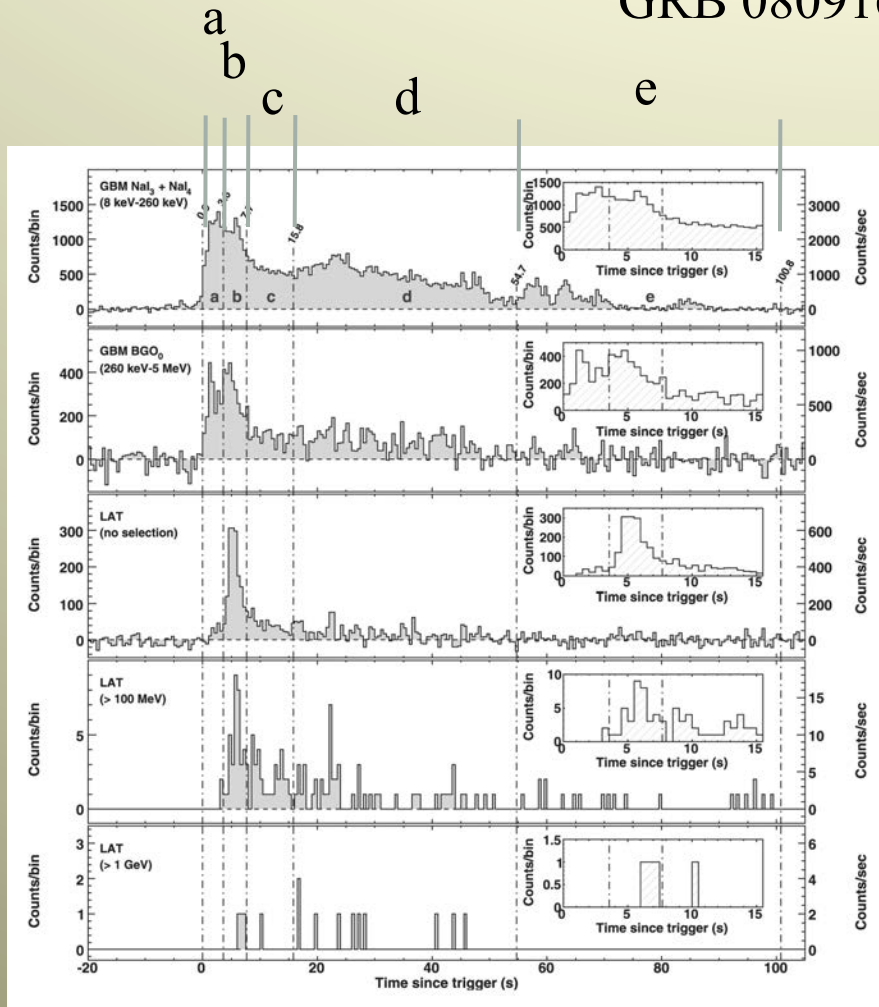


$32 < t < 72$

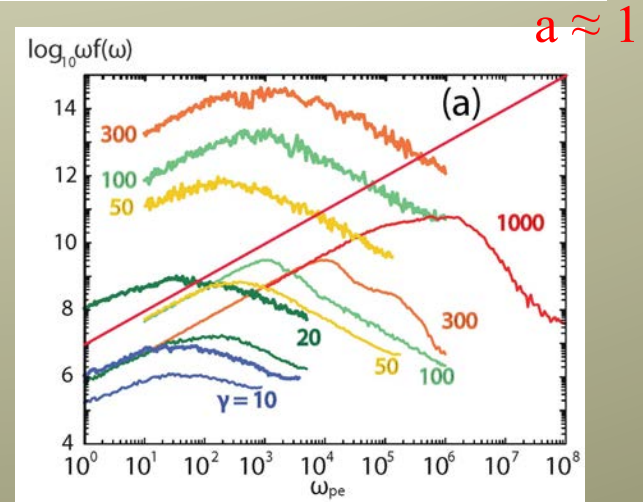
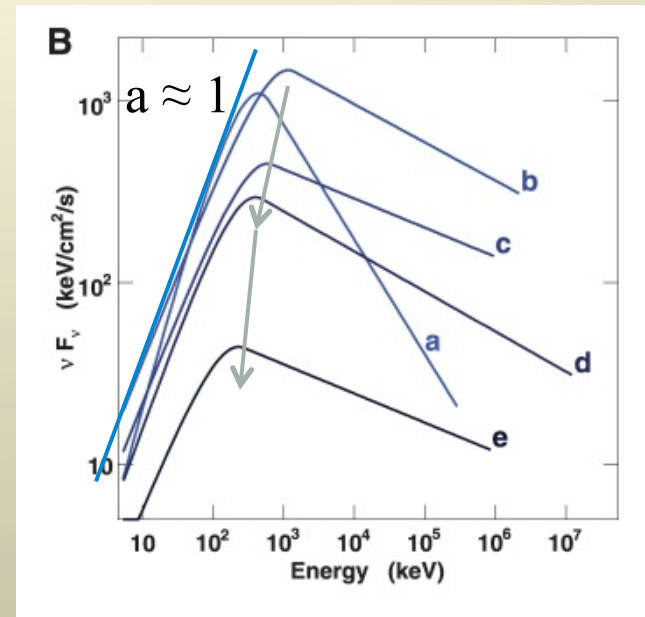


# Observations and numerical spectrum

GRB 080916C



Abdo et al. 2009, Science



Nishikawa et al. 2010

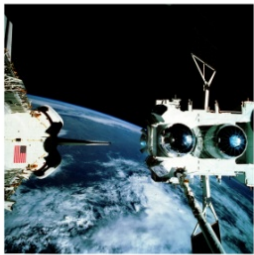
# *Summary*

- Reconnection is ubiquitous in magnetosphere, solar, and astrophysical plasmas
- Reconnection release Poynting flux to kinetic energy
- Particles are accelerated by reconnection
- Reconnection may provide additional time variability in radiation and involve in spectrum evolution and its structure
- Reconnection near compact objects may contribute to particle acceleration

# **Gamma-Ray Large Area Space Telescope (*FERMI*)**

*(launched on June 11, 2008)* <http://fermi.gsfc.nasa.gov/>

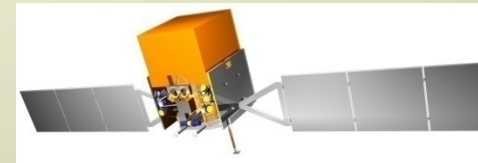
Compton Gamma-Ray  
Observatory (CGRO)



Burst And Transient  
Source Experiment

(BATSE) (1991-2000)

PI: Jerry Fishman



Fermi (GLAST)

*All sky monitor*

- ⦿ Large Area Telescope (LAT) PI: Peter Michaelson:  
gamma-ray energies between 20 MeV to about 300 GeV
- ⦿ Fermi Gamma-ray Burst Monitor (GBM) PI: Bill Paciaas  
(UAH) (Chip Meegan (Retired;USRA)): X-rays and gamma  
rays with energies between 8 keV and 25 MeV

(<http://gammaray.nsstc.nasa.gov/gbm/>)

*The combination of the GBM and the LAT provides a powerful tool for studying radiation from relativistic jets and gamma-ray bursts, particularly for time-resolved spectral studies over very large energy band.*

# ***Structure of Tristan code: Subroutines***

Main program

- main loop

- dump data for rerun and diagnostics

- accumulate data for radiation

input program (include)

- set parameters for simulations (density, jet velocity, magnetic field, etc)

- load particles as initial conditions

diagnostic program (include) (not active)

# *Initial settings*

## Jet simulations

c number of processors

parameter (Nproc=4)

parameter (Npx=1,Npy=2,Npz=2)

c VIRTUAL PARTICLE array is distributed among processes so that each process  
c works on  $nFx \cdot nFy \cdot nFz$  cells (its subdomain);

c !!! y and z domain size MUST BE EQUAL in the present setup:  $nFy = nFz$  !!!

c FIELD arrays have  $mFi$  ( $mFx, mFy, mFz$ ) elements in each dimension:

c  $nFi$  plus 3 ghost cells on the "Right" and 2 ghost cells on the "Left"

parameter (mx=645,my=11,mz=11)

parameter ( $nFx = (mx - 5) / Npx, mFx = nFx + 5$ )

parameter ( $nFy = (my - 5) / Npy, mFy = nFy + 5$ )

parameter ( $nFz = (mz - 5) / Npz, mFz = nFz + 5$ )

c depending the size of domain in a processor

parameter (nptl=2000000)

parameter (mb=nptl,mj=1800000)

c size of particle communication buffer arrays

c \*\* size is set as for ambient particles that move in one general direction \*\*

c !! check for particle number moving perpendicular to jet flow in Left proc. !!

c \*\* mpass = nFy\*nFz\*c\*DT\*adens + 10%-20% \*\*

c \*\* must be reset for different particle densities \*\*

parameter (mpass=500000)

parameter (mdiag=2500)

c 2\*\*15-1

parameter (imax=32767)

integer size,myid,ierror

integer lgrp,comm3d

integer topol

integer dims(3),coords(3)

logical isperiodic(3),reorder

integer FBDRx,FBDRy,FBDRz

integer FBDLx,FBDLy,FBDLz

integer FBDRxe,FBDLxe

integer FBDRxp,FBDLxp

integer FBD\_BRx,FBD\_BRy,FBD\_BRz

integer FBD\_BLx,FBD\_BLy,FBD\_BLz

integer FBD\_ERx,FBD\_ERY,FBD\_ERz

integer FBD\_ELx,FBD\_ELy,FBD\_ELz

c temporary arrays in 16-bit integers for data dump

integer\*2 irho,ifx,ify,ifz,ixx,iyy,izz

real mi,me

character strb1\*6,strb2\*6,strb3\*6,strb4\*6,strb5\*6,strb6\*6  
character strj1\*6,strj2\*6,strj3\*6,strj4\*6,strj5\*6,strj6\*6  
character strfb\*5,strfe\*5  
character strin\*8  
character dir\*28,num\*3,st01,st02,st03,st0\*3,st\*4,hyph  
character step\*6,step1,step2,step3,step4,step5  
character south\*3,soute\*3,soutd\*5,soutv\*4  
character ndiag\*6,nfield\*7  
character num1,num2,num3  
character strpd\*6

c electric and magnetic field arrays

dimension ex(mFx,mFy,mFz),ey(mFx,mFy,mFz),ez(mFx,mFy,mFz)  
dimension bx(mFx,mFy,mFz),by(mFx,mFy,mFz),bz(mFx,mFy,mFz)

c electric field longitudinal increaments (currents) arrays

dimension dex(mFx,mFy,mFz),dey(mFx,mFy,mFz),dez(mFx,mFy,mFz)

c ambient ions and electrons positions and velocities arrays

dimension xi(mb),yi(mb),zi(mb),ui(mb),vi(mb),wi(mb)  
dimension xe(mb),ye(mb),ze(mb),ue(mb),ve(mb),we(mb)

c jet ions and electrons positions and velocities arrays

dimension xij(mj),yij(mj),zij(mj),uij(mj),vij(mj),wij(mj)

dimension xej(mj),yej(mj),zej(mj),uej(mj),vej(mj),wej(mj)

c diagnostic arrays (for quantities recorded on the grid)

cWR dimension flx(mFx,mFy,mFz),fly(mFx,mFy,mFz),flz(mFx,mFy,mFz)

cWR dimension rho(mFx,mFy,mFz)

c diagnostic arrays for velocity distribution

dimension Cvpar(mdiag),Cvper(mdiag),xpos(mdiag)

c integer\*2 arrays

dimension ifx(mFx,mFy,mFz),ify(mFx,mFy,mFz),ifz(mFx,mFy,mFz)

dimension irho(mFx,mFy,mFz)

dimension ixx(mb),iyy(mb),izz(mb)

c temporary arrays for jet injection

c dimension Cseli(msel),Csele(msel)

dimension ipsend(4),iprecv(Nproc\*4)

```
cCOL embed "topology" calculation
  dimension itops(3),itopr(Nproc*3)
  dimension topol(0:(Nproc-1),3)
```

```
c smoother array
```

```
  dimension sm(-1:1,-1:1,-1:1)
```

```
c smoother arrays for combined digital filtering
```

```
  dimension sm1(-1:1,-1:1,-1:1),sm2(-1:1,-1:1,-1:1)
```

```
  dimension sm3(-1:1,-1:1,-1:1)
```

```
  dimension nfilt(16)
```

```
c initialize MPI
```

```
c ** "size" must be equal "Nproc"; "myid" is a ID for each process **
```

```
  common /pparms/ lgrp,comm3d
```

```
  lgrp = MPI_COMM_WORLD
```

```
  call MPI_INIT(ierror)
```

```
  call MPI_COMM_SIZE(lgrp,size,ierror)
```

```
  call MPI_COMM_RANK(lgrp,myid,ierror)
```

```
c define virtual topology - assign processes to the domains
c 3D Cartesian decomposition
c number of processes in each direction
    dims(1)=Npx
    dims(2)=Npy
    dims(3)=Npz
c indicate whether the processes at the "ends" are connected
c ** y and z directions are periodic **
cJET
    isperiodic(1)=.false.
    isperiodic(2)=.true.
    isperiodic(3)=.true.
c changing "reorder" to .true. allows MPI to reorder processes for better
c performance - in accordance to the underlying hardware topology
    reorder    =.false.
c number of dimensions
    ndim=3
```

```

c create Cartesian decomposition
c new communicator "comm3d" created - it must be used for communication
c ** in test simulations processes in "comm3d" have the same rank as in **
c ** MPI_COMM_WORLD (is this feature portable to different computers?) **
    call MPI_CART_CREATE(lgrp,ndim,dims,isperiodic,reorder,
        &                                comm3d,ierror)

c find Cartesian coordinates of the process (one can use also "MPI_CART_GET")
c ** coordinates run from 0 to Npi-1 **
    call MPI_CART_COORDS(comm3d,myid,3,coords,ierror)
c    call MPI_CART_GET(comm3d,3,dims,isperiodic,coords,ierror)

c find ID of the (6) neighbors to the process (through the surfaces)
c ** communication is set up in the way that it requires contacting 6 closest **
c ** neighbors only **
c ** second argument in "MPI_CART_SHIFT" is direction, third is shift=1 **
    call MPI_CART_SHIFT(comm3d,0,1,nleft,nright,ierror)
    call MPI_CART_SHIFT(comm3d,1,1,nfront,nrear,ierror)
    call MPI_CART_SHIFT(comm3d,2,1,nbottom,ntop,ierror)

```

```
if (nFy.ne.nFz) then
```

```
  if (myid.eq.1) print *, 'Y and Z DOMAIN SIZES MUST BE EQUAL !!!'
```

```
  goto 9999
```

```
end if
```

```
call smoother(sm)
```

c defining the characters for filenames

```
strfb = 'fldb_'
```

```
strfe = 'flde_'
```

```
strb1 = 'pambx_'
```

```
strb2 = 'pamby_'
```

```
strb3 = 'pambz_'
```

```
strb4 = 'pambu_'
```

```
strb5 = 'pambv_'
```

```
strb6 = 'pambw_'
```

```
strj1 = 'pamjx_'  
strj2 = 'pamjy_'  
strj3 = 'pamjz_'  
strj4 = 'pamju_'  
strj5 = 'pamjv_'  
strj6 = 'pamjw_'
```

```
strin = 'inparam_'
```

c diagnostics and partial output files

```
soutb = 'bf_'
```

```
soute = 'ef_'
```

c   soutd = 'dens\_'

```
soutd = 'diag_'
```

```
soutv = 'vel_'
```

c continued